

REVISTA IBRACON DE ESTRUTURAS E MATERIAIS IBRACON STRUCTURES AND MATERIALS JOURNAL

Analysis and validation of correlation curves between sclerometry and compression tests for the evaluation of compressive strength of concretes

Análise e validação de curvas de correlação entre a esclerometria e ensaios de compressão para avaliação da resistência à compressão de concretos







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Abstract

The present work consists in obtaining correlation curves between compressive tests and sclerometry tests from an extensive experimental program comprising 630 concrete cylindrical samples cast in laboratory, employing materials and methods available in Brazil. The concretes, with compressive strengths ranging from 20~MPa to 50~MPa, were submitted to sclerometry tests and mechanical compressive tests. The results were used to obtain correlation curves. which were adopted in measurements of structural elements molded in a construction site, indicating that the curves provided by the equipment manufacturer are not suitable for the material in study. This is the first stage of a broader study aiming to contribute to the improvement of the Brazilian code regulating the application of the sclerometry to obtain concrete compressive strength.

Keywords: concrete, sclerometry, compressive strength, correlation curves.

Resumo

Este trabalho consiste na obtenção de curvas de correlação entre ensaios mecânicos e testes de esclerometria a partir de um programa experimental extenso realizado em 630 corpos de prova de concreto. empregando materiais e métodos disponíveis no Brasil. Os concretos, com resistências a compressão variando de 20 MPa a 50 MPa, foram submetidos a ensaios de esclerometria e a testes mecânicos de compressão, cujos resultados foram empregados na obtenção de curvas de correlação. Tais curvas foram adotadas em medições de elementos estruturais moldados em um canteiro de obras, indicando que as curvas fornecidas pelo fabricante do equipamento não são adequadas para o material em estudo. Trata-se da primeira etapa de um amplo estudo visando contribuir para o aprimoramento das normas brasileiras que estabelecem os procedimentos para a aplicação da esclerometria para medir a resistência a compressão de concreto.

Palavras-chave: concreto, esclerometria, resistência a compressão, curva de correlação.

Received: 04 Apr 2017 • Accepted: 05 Apr 2018 • Available Online:

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1. Introduction

Non-Destructive Tests (NDT) are considered as important tools for the structural and quality evaluations of construction elements. Concerning mechanical properties of concrete structures in service conditions it is quite convenient to adopt in situ techniques that do not demand carroting, both for economical and safety reasons, since extracting samples from structural elements may cause deterioration and/or affect the serviceability or the entire structure. These facts certainly contributed to spreading the application of non-destructive techniques, such as the sclerometry, all over the world (Breysse et al [11], Fan et al [13], Fort et al [14], Sardar et al [18]).

The sclerometer measures essentially the hardness of the surface. The method is based on the rebound principle, in which an elongated spring, upon returning to the equilibrium position, causes a hammer with a certain mass to move colliding against the surface of an object with a much larger mass. After the impact the deformation of the spring is measured through extensometers, present inside the apparatus. The measured deformation provides the sclerometric index, which is shown in the apparatus. With this index empirical correlations can be made with compression tests (Ayman and Mohamed [10]. Malhotra and Carino [16]). The device used herein (Figure 1(a)) was designed by the Swiss engineer Ernst Schmidt - so it is also known as Schmidt sclerometer. Nowadays its use is very widespread: it is estimated that up to 1986 had already been sold around fifty thousand sclerometers (Malhotra and Carino [16]). Each type of sclerometer provides a specific set of curves correlating sclerometry indexes to compressive strength values obtained via mechanical tests (Malhotra and Carino [16]). Figure 1(b) shows the correlation curves provided by the manufacturers of the employed sclerometer model N/NR where three shot directions are considered: horizontal, vertical downwards and vertical upwards. As one can see by looking at the curves, the results are considerably affected by the shot direction. However, it is well known that those curves do not fit a wide variety of concretes but are restricted to specific materials and test conditions. This fact is a handicap for the application of this procedure in a wide manner.

The present study consists of an extensive experimental program concerning two steps: firstly, 630 cylindrical concrete samples were fabricated and subjected to sclerometer and mechanical tests in order to obtain the correlation curves; secondly, measurements were performed in concrete structural members in a construction site, so as to reproduce a practical situation of material's verification and control under in situ conditions, and to compare the results obtained from the correlation curves to those measured via mechanical tests on cylindrical concrete samples for technological control purposes.

The aim of this work is contributing for the reliable application of sclerometry devices in Brazil, since the correlation curves provided by the commonly adopted equipments may not suit the local materials. Further, the related Brazilian Standard (ABNT NBR 7584:2012 - Concreto endurecido — Avaliação da dureza superficial pelo esclerômetro de reflexão - Método de ensaio) (ABNT [8]) does not provide detailed information concerning the assessment and application of adequate correlation curves, which limits the application of this technique for practical purposes.

2. Experimental program

Firstly, an extensive experimental study was developed so as to generate sufficient and reliable data. The experimental program comprised 7 classes of concrete samples identified as CXX, where XX indicates the compressive strength value specified in the pro-



Figure 1

(a) Sclerometer model N/NR; (b) Correlation curves provided by the manufacturer considering 3 shot application directions

Compositions (given in mass) adopted for the seven concrete sets

Concrete	f (MPa)	Artificial sand	Natural sand	BO	B1	w/c	Add. %	Cement kg/ m ³
C20	20	0.924	2.772	1.200	2.800	0.65	0.65	260
C25	25	0.843	2.528	1.117	2.607	0.60	0.65	280
C30	30	0.700	2.099	0.971	2.265	0.55	0.65	320
C35	35	0.644	1.933	0.914	2.133	0.52	0.65	340
C40	40	0.621	1.864	0.891	2.078	0.50	0.65	350
C45	45	0.611	1.832	0.880	2.052	0.45	0.65	360
C50	50	0.436	1.307	0.701	1.635	0.38	0.65	450
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B0: aggregates with diameter < 9.5mm; B1: aggregates with diameter< 19mm

Table 2

Aggregate's grading

Grading (ABNT [2])										
Diameter (mm)		% retained	(accumulated)							
Diameier (mm)	BO	B1	NS	AS						
25	-	-	-	-						
19	-	14	-	-						
12.5	-	77	-	-						
9.5	6	98	-	-						
6.3	60	99	1	-						
4.8	89	99	1	1						
2.4	99	99	4	22						
1.2	99	99	21	42						
0.6	99	99	58	53						
0.3	99	99	89	62						
0.15	99	99	98	76						
Bottom	100	100	100	100						
Specific mass (g/cm³) (ABNT [4]) (ABNT [5])	2.76	2.85	2.6	2.725						
Unity mass (g/cm³) (ABNT [1])	1.4	1.49	1.44	1.72						
Amount of fine materials (%) (ABNT [3])	0.685	0.945	2.25	20.8						
B0: aggregates with diameter < 9.5mm; B1: aggregates with diameter < 19mm; NS: natu	ural sand; AS: artificial sa	nd								

portioning specifications. Table 1 shows the mixture's proportions, pre-defined for compressive strengths ranging from 20 MPa to 50 MPa. All mixtures adopted cement type CPIIIE40, natural and artificial sand and polifunctional plastificant additive. Water/cement ratio ranged from 0.38 to 0.65.

All materials adopted in the concretes fabrication were characterized according to specific standardized tests – grading analysis, specific mass, amount of fine grains – for the sake of reproducibility. Mix proportions, as well as water/cement ratios, were defined in terms of aggregates grading and the amount of fine grains (diameter < 0.075mm) given in Table 2 (Mehta and Monteiro [17]). Following the pre-definition of mixture proportions, 11 cylindrical samples (100 x 200 mm according to NBR 5738 (ABNT [6])) per concrete class were molded aiming to verify the compressive strength values. Then 90 concrete cylindrical samples (100x200mm) per strength class, totalizing 630 specimens, were fabricated in order to obtain enough data for the analysis. Figure 2(a) illustrates the specimens' fabrication. The cylindrical samples were kept in molds for about 72 hours under controlled moisture conditions. then they were unmolded and kept under plain water as shown in Figure 2(b). At the age of 27 days, the specimens were taken off the water for surface regularization, as illustrated in Figure 2(c), and subjected to sclerometry and compressive tests 28 days after molding.

The Brazilian Standard NBR 7584 (ABNT [12]) states that a concrete specimen must be subjected to 16 impact points on its surface, defined as the nodes of a 3x3 mesh like the one shown in Figure 3(a). However, the present work adopted 4 impact points, as indicated in Figure 3(b), due to the small dimensions of the concrete cylinders in study.

For each mixture, 90 specimens were grouped into 3 sets of 30 samples. Each set was subjected to sclerometry measurements under one of the three shot directions indicated in Figure 4, identified herein as: Position 1 (\rightarrow) (Figure 4(a)); Position 2 (\downarrow) (Figure 4(b)) and Position 3 – (\uparrow) (Figure 4(c)). Mechanical uniaxial tests were also performed according to Brazilian Standard NBR 5739:2007 (ABNT [7]) for the evaluation of the compression strength (f_c), so as to provide sufficient data for analysis and validation purposes.





Figure 2

Fabrication of the concrete's specimens (a) water curing (b) and regularization of the top surfaces



Figure 3

(a) Mesh with 16 impact points as stated by NBR 7584:2012 (ABNT [12]) and (b) Mesh with 4 impact points, as adopted in the present study



Figure 4

Sclerometry test performed in three positions: (a) Position $1(\rightarrow)$ (b) vertical downwards (Position 2) and (c) vertical upwards (Position 3)

Table 3

Experimental data obtained for C20 concrete - Set 1

Item	Position	11	12	13	14	la	f _c (MPa)
1	Ļ	12	14	12	12	12.5	18.47
2	Ļ	14	14	14	14	14.0	20.66
3	Ļ	14	14	16	16	15.0	19.62
4	Ļ	16	14	16	16	15.5	20.54
5*	Ļ	15	15	14.5	14.5	14.8	20.66
6*	Ļ	13	13	14	14	13.5	21.16
7	Ļ	13	13	13	13	13.0	21.15
8	Ļ	14	12	12	13	12.8	23.81
9	Ļ	13.5	13	13	13	13.1	21.21
10	Ļ	18	13	13	13	13.0	25.64
11	↑	16	16	16	16	16.0	22.68
12*	↑	16	16	15	15	15.5	20.82
13	↑	16	15	15	17	15.8	23.53
14	↑	15	16	15	16	15.5	23.52
15	↑	16	16	16	16	16.0	25.68
16	↑	16	16	16	16	16.0	21.59
17		17	16	16	16	16.3	18.91
18		21	17	16	16	16.3	21.39
19	↑	15	15	14	15	14.8	22.61
20	↑	15	15	15	15	15.0	20.79
21	\rightarrow	14	14	14	14	14.0	22.04
22	\rightarrow	15	14	14	15	14.5	20.41
23	\rightarrow	14	14	14	15	14.3	18.47
24	\rightarrow	13	14	14	13	13.5	23.94
25	\rightarrow	16	16	16	15	15.8	24.23
26	\rightarrow	17	16	16	16	16.3	26.32
27	\rightarrow	14	14	14	14	14.0	17.32
28	\rightarrow	13	14	14	14	13.8	19.01
29	\rightarrow	13.5	13.5	13.5	14	13.6	14.69
30	\rightarrow	14	14	14	14	14.0	19.20
* Samples attai	ned rupture during	g E test; ** Discarde	ed values				

Information on the experimental measurements obtained from all tested samples are presented in Tables 3 to 23, where: I1, I2, I3 and I4 are the sclerometer index readings, obtained as described in section 1, I_a is the average index value, Position indicates the shot direction, fc is the compressive strength.

3. Results and discussions

3.1 I x f_c correlation curves

The database was treated using tests for Normal and Student distribution and Pearson correlation coefficient and Kolmogorov-Smirnov two sample tests were used as a measure of the quality of the correlation (Figueiredo Filho and Silva [15]). The analysis and validation of the curves were done with the help of the python programming language, using the numpy, scipy and pandas packages for the numerical and statistical processing. Detailed information concerning the database and correlation analysis is available in Botelho et al [11]. According to Figure 5, in all the ranges of fc it is observed that the distribution of the values in Position 3 (\uparrow) presents higher sclerometer indices than in Position 2 (\downarrow). Observing the diagram of Figure 5, it can be seen that the mean values of the sclerometer index (I) increase with the fc ranges, suggesting a linear behavior. In addition to that, the three directions present different mean values, Position 3 (\uparrow) having the highest one, followed by Position 1 (\rightarrow) and Position 2 (\downarrow).

The linear regression models of the form $f_c = al + b$ for the sclerometer index as a function of each of the shot directions are presented in Table 24. The MSE column indicates the mean square error, the R column indicates the Pearson correlation coefficient and the p column indicates the p-value associated with the regression model. The same data is plot on Figure 6, which allows the graphical comparison of the linear regression models for the sclerometer index as a function of the shot directions. One can compare the trend lines obtained for the three adopted directions. which respect a certain distance from each other.

Table 4

Experimental data obtained for C20 concrete samples - Set 2

Item	Position	11	12	13	14	la	f _c (MPa)
31	Ļ	14	14	13	13	13.5	17.67
32	Ļ	14	13	13	14	13.5	17.65
33	Ļ	12.5	12.5	13	13	12.8	16.04
34	Ļ	12.5	12.5	12.5	12	12.4	17.55
35	Ļ	12.5	12.5	12	12	12.3	18.23
36	Ļ	10**	14.5	14.5	13.5	14.2	18.51
37	Ļ	13	13	13	13	13.0	17.72
38	Ļ	13	13	13	17**	13.0	19.12
39	Ļ	13.5	12.5	13.5	13.5	13.3	18.92
40	Ļ	14	14	13	13	13.5	19.30
41	↑	17	16	16	17	16.5	17.14
42	↑	16.5	15.5	16.5	10**	16.2	17.83
43	↑	16	16	16	16	16.0	17.49
44	↑	16	16	16	16	16.0	17.57
45	↑	16	16	16	15	15.8	17.77
46	↑	15.5	16	16	16	15.9	18.25
47	↑	15	15.5	15.5	15.5	15.4	20.12
48	↑	16	16	16	16	16.0	19.40
49	↑	16	16	16	16.5	16.1	20.22
50	↑	16	16	15	15	15.5	19.43
51	\rightarrow	14	14	14	14.5	14.1	18.03
52	\rightarrow	16	15	15	16	15.5	19.20
53	\rightarrow	13.5	14	15	10**	14.2	18.49
54	\rightarrow	14	15	15	15	14.8	17.94
55	\rightarrow	14	14	13	14	13.8	18.72
56	\rightarrow	13	13.5	14.5	20**	13.7	17.84
57	\rightarrow	14	14	13	13	13.5	18.89
58	\rightarrow	13.5	13.5	12.5	12.5	13.0	18.00
59	\rightarrow	14	14	14	14	14.0	19.63
60	\rightarrow	14	14	14	14	14.0	20.09
** Discarded vo	alues		~				

Table 5 Experimental data obtained for C20 concrete samples - Set 3

Item	Position	11	12	13	14	la	f _c (MPa)
61	Ļ	14	14	14	14	14.0	18.95
62	\downarrow	15	15	15	15	15.0	19.40
63	\downarrow	15	15	15	15	15.0	19.51
64	\downarrow	14	14	15	15	14.5	18.13
65	\downarrow	16	15	15	16	15.5	19.38
66	\downarrow	15	15	15	15	15.0	19.96
67	\downarrow	14	14	14	14	14.0	19.63
68	Ļ	16	16	16	16	16.0	19.48
69	\downarrow	17	17	16	16	16.5	20.45
70	\downarrow	15	15	14	14	14.5	17.80
71	↑	16	17	16	17	16.5	19.51
72	↑	16	16	16	16	16.0	19.57
73	↑	16.5	16	15	15.5	15.8	18.26
74	↑	15.5	15.5	14	14.5	14.9	18.54
75	↑	16.5	16	16	10**	16.2	19.46
76	↑	17.5	17	16	16.5	16.8	20.35
77	1	16	16	15	15	15.5	18.87
78	↑	17	17.5	16	16.5	16.8	19.20
79	↑	12**	16	16	16.5	16.2	19.33
80	↑	15	15	15	15	15.0	18.16
81	\rightarrow	14	14	14	14	14.0	18.13
82	\rightarrow	17	16	16	17	16.5	20.32
83	\rightarrow	15.5	15.5	15.5	15.5	15.5	18.44
84	\rightarrow	17	17	16	16	16.5	18.18
85	\rightarrow	14	14	19**	14.5	14.2	18.28
86	\rightarrow	14	14	14	14	14.0	20.27
87	\rightarrow	16	16	15	15	15.5	19.40
88	\rightarrow	15.5	15.5	15.5	15.5	15.5	19.12
89	\rightarrow	15	15	15	15	15.0	18.67
90	→	14	14.5	13	13.5	13.8	19.89
** Discardod va							

Discarded value

Experimental data obtained for C25 concrete samples - Set 1

Item	Position	11	12	13	14	la	f _c (MPa)
1	\downarrow	17	17	17	17	17.0	23.15
2	\downarrow	17	17	16	16	16.5	25.38
3	\downarrow	16	16	16	16	16.0	27.81
4	\downarrow	18	18	18	18	18.0	24.87
5*	\downarrow	19	19	19	19	19.0	24.87
6	\downarrow	16	15.5	16	16	15.9	26.17
7	\downarrow	15	15	15	15	15.0	23.40
8	\downarrow	16	16	17	17	16.5	22.41
9	Ļ	16.5	16.5	16.5	17	16.6	26.10
10	Ļ	15	15	15	15	15.0	24.64
11	↑	21	21	21	21	21.0	22.84
12	↑	21	21	21	21	21.0	23.35
13	↑	19	19	19	19	19.0	22.63
14	↑	19	19	19	19	19.0	24.09
15	↑	19	19	19	19	19.0	26.47
16	↑	19.5	19.5	19.5	20	19.6	22.51
17	↑ (22	22	22.5	14**	22.2	24.04
18	↑ (22.5	22.5	22.5	23	22.6	25.17
19	↑	22	22	22	22	22.0	22.70
20	↑	22	22	22	21	21.8	26.69
21	\rightarrow	19	19	19	19	19.0	23.69
22	\rightarrow	18	18	18	18	18.0	23.67
23	\rightarrow	18	18	18	18	18.0	22.52
24	\rightarrow	18	18	18	18	18.0	22.80
25	\rightarrow	17	17	17	17	17.0	23.55
26	\rightarrow	17.5	17.5	17.5	17.5	17.5	25.31
27	\rightarrow	17	17.5	17.5	17	17.3	22.13
28	\rightarrow	17	17	17	16.5	16.9	23.10
29	\rightarrow	17	17	17	17.5	17.1	23.30
30	\rightarrow	18	18	18	18	18.0	24.71
* Sample attain	ed rupture during	E test; * * Discarde	d value				

Experimental data obtained for C25 concrete samples - Set 2

Item	Position	11	12	13	14	la	f _c (MPa)
31	\downarrow	17	17	17	17	17.0	25.02
32	\downarrow	17	17	17	17	17.0	22.98
33	\downarrow	17	17	17	17	17.0	25.07
34	\downarrow	18	18	18	18	18.0	24.01
35	\downarrow	18	18	17	17	17.5	23.39
36	\downarrow	18	18	17.5	17	17.6	24.50
37	\downarrow	18	18	18	28**	18.0	21.93
38	\downarrow	19	19	19	19	19.0	22.57
39	\downarrow	19	19	18	18	18.5	24.76
40	\downarrow	17	17	16	16	16.5	23.05
41	1	20	20	20	20	20.0	23.98
42	1	22	22	22	22	22.0	23.35
43	1	22	22	22	22	22.0	23.43
44	1	21	21	21	21	21.0	24.70
45	1	21	21	22	22	21.5	24.60
46	1	21	21	20.5	20	20.6	22.08
47	1	21	21	22	22	21.5	23.31
48	1	21	21	21	21	21.0	24.99
49	1	22	22	22	22	22.0	25.50
50	1	18	18	18	18	18.0	22.56
51	\rightarrow	19	19	19	19	19.0	24.70
52	\rightarrow	18	18	18	18	18.0	22.12
53	\rightarrow	19	19	19	19	19.0	24.00
54	\rightarrow	20	20	20	20	20.0	22.96
55	\rightarrow	18	18	18	18	18.0	22.74
56	\rightarrow	18	18	18	18	18.0	23.61
57	\rightarrow	18	18	19	19	18.5	23.54
58	\rightarrow	20	20	19.5	19.5	19.8	24.06
59	\rightarrow	20	20	21	21	20.5	23.39
60	\rightarrow	17	17	17	17	17.0	24.54
** Discarded vo	llue						

Experimental data obtained for C25 concrete samples - Set 3

Item	Position	11	12	13	14	la	f _c (MPa)
61	\downarrow	18	18	18	18	18.0	23.69
62	\downarrow	18	18	18	18	18.0	22.75
63	\downarrow	18	18	18	18	18.0	23.95
64	\downarrow	17	17	17	17	17.0	24.37
65	\downarrow	17	17	18	18	17.5	22.91
66	\downarrow	18	18	17.5	17.5	17.8	25.02
67	\downarrow	19	19	20	20	19.5	24.87
68	\downarrow	19	19	19	19	19.0	25.71
69	Ļ	19	19	19	19	19.0	25.24
70	Ļ	19	19	19	15**	19.0	22.05
71	1	21	21	21	21	21.0	25.78
72	↑	21	21	21	21	21.0	23.24
73	↑	21	21	21	21	21.0	25.30
74	↑	20	20	20	20	20.0	22.12
75	1	20	20	21	21	20.5	25.27
76	↑	22	22	23	23	22.5	23.86
77	1	20	20	21	21	20.5	24.92
78	1	22	22	22	22	22.0	23.20
79	1	21	21	21	21	21.0	25.35
80	1	18	18	18	18	18.0	25.34
81	\rightarrow	18	18	18	18	18.0	23.38
82	\rightarrow	18	18	18	18	18.0	24.13
83	\rightarrow	19	19	20	20	19.5	26.02
84	\rightarrow	20	20	19.5	19.5	19.8	25.46
85	\rightarrow	17	17	16.5	16.5	16.8	22.78
86	\rightarrow	16	16	16	16	16.0	26.67
87	\rightarrow	18	18	18	18	18.0	23.48
88	\rightarrow	16	18	16	18	17.0	22.49
89	\rightarrow	17	17	17	17	17.0	25.35
90	\rightarrow	19	19	19	19	19.0	24.06
** Discarded vo	lue						

Experimental data obtained for C30 concrete samples - Set 1

Item	Position	11	12	13	14	la	f _c (MPa)
1	\downarrow	19	19	19	19	19.0	28.14
2	\downarrow	19	19	21	21	20.0	28.83
3	\downarrow	20	21	21	20	20.5	28.02
4	\downarrow	18	18	18	17.5	17.9	28.02
5*	\downarrow	18	18	17.5	17.5	17.8	30.28
6*	\downarrow	18	18	18	18	18.0	28.69
7	\downarrow	18	18	18	18	18.0	27.02
8	\downarrow	20	20	18	18	19.0	32.05
9	Ļ	19	19	19	19	19.0	28.01
10	Ļ	18.5	19	18.5	19	18.8	29.13
11*	1	22	22	23	23	22.5	28.62
12	1	24	24	23	23	23.5	28.93
13	1	23	23	23	23	23.0	27.95
14	1	23	23	23	23	23.0	32.19
15	1	24	24	22	22	23.0	32.65
16	1	24	24	24	24	24.0	26.88
17	1	24	24	24	24	24.0	33.82
18	1	22	22	21.5	21.5	21.8	29.63
19	1	21.5	22	21.5	22	21.8	34.33
20	1	22	22	22	22	22.0	30.84
21	\rightarrow	20	20	20	20	20.0	32.11
22	\rightarrow	20	20	20	20	20.0	29.20
23	\rightarrow	19	19	19	19	19.0	28.75
24	\rightarrow	19	19	19	19	19.0	29.35
25	\rightarrow	21	21	20	20	20.5	26.97
26	\rightarrow	21	21	20	20	20.5	27.02
27	\rightarrow	21	21	21	21	21.0	28.84
28	\rightarrow	20	20	19.5	19.5	19.8	31.37
29	\rightarrow	20	20	20	20	20.0	29.00
30	\rightarrow	19	19	19	19	19.0	34.43
* Samples attair	ned rupture during	g E test					

Item	Position	11	12	13	14	la	f _c (MPa)
31	\downarrow	18	18	18	18	18.0	29.42
32	\downarrow	20	20	20	20	20.0	29.26
33	Ļ	19	19	19	19	19.0	27.07
34	Ļ	20	18	18	20	19.0	26.71
35	Ļ	19	19	19	19	19.0	28.81
36	Ļ	21	21	21	21	21.0	34.06
37	Ļ	20	20	19.5	19.5	19.8	26.97
38	Ļ	20	19.5	19.5	19.5	19.6	29.67
39	Ļ	20	20	20	20	20.0	34.39
40	Ļ	20	20	20	20	20.0	29.44
41	↑	24	24	24	24	24.0	35.63
42	↑	24	24	24	24	24.0	27.31
43	↑	24	24	24	24	24.0	31.74
44	↑	24	24	23	23	23.5	28.02
45	↑	21	21	21	21	21.0	35.23
46	↑	22	22	21	21	21.5	35.14
47	↑	23	23	23	23	23.0	30.26
48	↑	23	23	23	23	23.0	29.08
49	↑ (24	24	24	24	24.0	32.11
50	↑	24	24	23	23	23.5	33.17
51	\rightarrow	20	20	20	20	20.0	31.22
52	\rightarrow	20	20	20	20	20.0	33.44
53	\rightarrow	19	19	21	21	20.0	32.19
54	\rightarrow	19	19	19	19	19.0	29.82
55	\rightarrow	19	19	19	19	19.0	29.69
56	\rightarrow	19	19	19	19	19.0	32.05
57	\rightarrow	23	23	22	22	22.5	32.12
58	\rightarrow	23	23	22.5	22.5	22.8	33.14
59	\rightarrow	21.5	21.5	21.5	22	21.6	29.09
60	, ,	20	20	20	20	20.0	33 10

Table 10Experimental data obtained for C20 concrete samples - Set 2

Item	Position	11	12	13	14	la	f _c (MPa)
61	\downarrow	19	19	19	14**	19.0	29.36
62	\downarrow	19	19	19	19	19.0	26.88
63	\downarrow	19	19	19	19	19.0	32.91
64	\downarrow	20	20	20	20	20.0	28.14
65	Ļ	20	20	20	20	20.0	29.34
66	Ļ	20	20	20	20	20.0	31.23
67	Ļ	18.5	18.5	19	19	18.8	32.38
68	Ļ	18	18	18	18	18.0	31.36
69	Ļ	18	18	18	18	18.0	31.61
70	Ļ	19	19	19	19	19.0	32.63
71	↑	23	23	23	23	23.0	31.89
72	↑	23	23	23	23	23.0	30.71
73	↑	23	23	23	23	23.0	32.66
74	↑	24	24	24	24	24.0	31.59
75	↑	25	25	25	25	25.0	27.12
76	↑	24.5	24.5	24.5	24.5	24.5	28.79
77	↑	24	24	24	24	24.0	27.22
78	↑	23	22	22	22.5	22.4	27.51
79	↑	23	22	22	22	22.3	32.07
80	↑	22	22	22	22	22.0	29.53
81	\rightarrow	20	20	20	20	20.0	27.54
82	\rightarrow	20	20	20	20	20.0	31.87
83	\rightarrow	20	20	20	20	20.0	31.67
84	\rightarrow	19	19	19	19	19.0	28.34
85	\rightarrow	20	20	20	20	20.0	28.74
86	\rightarrow	19	19	19	19	19.0	33.19
87	\rightarrow	20	20	20	20	20.0	31.08
88	\rightarrow	20	20	20	20	20.0	32.06
89	\rightarrow	20	20	20	20	20.0	31.82
90	\rightarrow	19	19	19	19	19.0	31.95

Table 11Experimental data obtained for 30 concrete samples – Set 3

Experimental data obtained for C35 concrete samples - Set 1

Item	Position	11	12	13	14	la	f _c (MPa)
1	\downarrow	20	20	20	20	20.0	34.49
2	\downarrow	21	21	21	21	21.0	34.58
3	\downarrow	21	21	21	21	21.0	33.64
4	\downarrow	21	21	21	21	21.0	34.54
5	\downarrow	20	20	20	20	20.0	35.89
6	\downarrow	22	22	22	22	22.0	35.88
7	\downarrow	20	20	21	21	20.5	33.33
8	\downarrow	21	21	22	22	21.5	34.17
9	\downarrow	21.5	21.5	22	22	21.8	36.15
10	\downarrow	20	20	20	20	20.0	36.90
11	1	24	24	24	24	24.0	36.71
12*	1	24	24	24	24	24.0	34.10
13	1	25	25	25	25	25.0	35.04
14	1	25	25	25	25	25.0	34.29
15	1	27	27	27	27	27.0	34.67
16	1	27	27	27	27	27.0	32.34
17	1	25	25	25	25	25.0	34.10
18	1	24	24	24	24	24.0	32.24
19	1	24	24	24	24	24.0	36.11
20	1	24	24	24	24	24.0	35.59
21	\rightarrow	22	22	22	22	22.0	32.02
22*	\rightarrow	22	22	22	22	22.0	32.20
23	\rightarrow	22	22	22	22	22.0	35.63
24*	\rightarrow	21	21	21	21	21.0	37.70
25	\rightarrow	20	20	20	20	20.0	33.84
26	\rightarrow	23	22.5	22	22	22.4	32.09
27	\rightarrow	23	23	23	23	23.0	35.52
28	\rightarrow	23.5	23	23	23	23.1	34.98
29	\rightarrow	23	23	23	23	23.0	34.80
30	\rightarrow	22	22	22	22	22.0	37.93
* Samples attair	ned rupture during	g E test; * * Discarde	ed values				

Experimental data obtained for C35 concrete samples – Set 2

Item	Position	11	12	13	14	la	f _c (MPa)
31	\downarrow	21	21	21	21	21.0	36.75
32	\downarrow	21	21	21	10**	21.0	32.93
33	\downarrow	23	23	23	23	23.0	34.12
34	\downarrow	21	21	21	21	21.0	35.22
35	Ļ	20	20	20	20	20.0	36.73
36	\downarrow	19	19	19	19	19.0	35.49
37	\downarrow	18	18	18	18	18.0	33.00
38	\downarrow	17	17	17	17	17.0	36.15
39	\downarrow	20	20	20	20	20.0	34.35
40	Ļ	20	20	20	20	20.0	34.58
41	1	25	25	25	25	25.0	36.63
42	1	25	25	25	25	25.0	37.56
43	1	26	24	26	24	25.0	35.15
44	1	27	27	27	27	27.0	33.32
45	1	26	26	26	26	26.0	36.38
46	1	26	26	26	26	26.0	33.05
47	1	26	26	26	26	26.0	32.61
48	1	24	24	24	24	24.0	33.54
49	1	24	24	23.5	23.5	23.8	32.72
50	1	23	23	23	23	23.0	36.27
51	\rightarrow	23	23	23	23	23.0	32.84
52	\rightarrow	23	23	23	23	23.0	34.89
53	\rightarrow	23	23	23	23	23.0	36.63
54	\rightarrow	22	22	22	22	22.0	35.75
55	\rightarrow	21	21	21	21	21.0	32.84
56	\rightarrow	20	20	20	20	20.0	32.34
57	\rightarrow	20.5	20.5	21	21	20.8	32.37
58	\rightarrow	20	20	21	21	20.5	32.43
59	\rightarrow	22	22	22	22	22.0	36.86
60	\rightarrow	22	22	22	22	22.0	34.40
** Discarded vo	lues						

Experimental data obtained for 35 concrete samples - Set 3

Item	Position	11	12	13	14	la	f _c (MPa)
61	\downarrow	22	22	22	22	22.0	34.11
62	Ļ	19	19	19	19	19.0	36.90
63	\downarrow	21	21	19	19	20.0	36.90
64	\downarrow	20	20	20	20	20.0	35.80
65	\downarrow	20	20	20	20	20.0	34.45
66	\downarrow	22	22	22	22	22.0	36.27
67	Ļ	22	22	20	20	21.0	32.20
68	Ļ	20	20	20	20	20.0	34.82
69	Ļ	20	20	20	20	20.0	34.39
70	Ļ	20	20	20	20	20.0	33.61
71	↑	25	25	25	25	25.0	36.39
72	↑	25	25	25	25	25.0	33.51
73	↑	25	25	25	25	25.0	35.27
74	↑	24	24	24	24	24.0	34.29
75	↑ (24	24	25	25	24.5	34.28
76	↑ (26	26	26	26	26.0	32.31
77	↑	26	26	26	26	26.0	34.43
78	↑	24.5	24.5	25	25	24.8	35.97
79	↑	25	25	25	25	25.0	36.58
80	↑ (25	25	25	25	25.0	34.78
81	\rightarrow	23	23	23	23	23.0	32.25
82	\rightarrow	21	23	23	21	22.0	35.99
83	\rightarrow	22	22	22	22	22.0	35.60
84	\rightarrow	22	22	22	22	22.0	33.38
85	\rightarrow	23	23	23	23	23.0	32.75
86	\rightarrow	23	23	23	23	23.0	36.72
87	\rightarrow	20	20	20	20	20.0	37.23
88	\rightarrow	21.5	21.5	21.5	21.5	21.5	34.64
89	\rightarrow	22	22	22	22	22.0	34.39
90	\rightarrow	20	20	21	21	20.5	36.05

Experimental data obtained for C40 concrete samples - Set 1

Item	Position	11	12	13	14	la	f _c (MPa)
1*	\downarrow	23	23	23	23	23.0	37.96
2	\downarrow	23	23	24	24	23.5	40.65
3	\downarrow	23	23	23	23	23.0	36.38
4	\downarrow	23	23	23	23	23.0	38.25
5	\downarrow	24	24	24	24	24.0	41.14
6	\downarrow	25	25	25	25	25.0	37.64
7	\downarrow	25	25	25	25	25.0	39.72
8	\downarrow	25	25	25	25	25.0	41.42
9*	\downarrow	24	24	25	25	24.5	27.49
10	Ļ	23	23	23	23	23.0	42.41
11	1	27	27	27	27	27.0	39.43
12	1	27	27	29	29	28.0	39.89
13	1	30	30	30	30	30.0	39.80
14	1	30	30	30	30	30.0	38.38
15	1	30	30	30	30	30.0	38.80
16	1	29	29	29	29	29.0	39.94
17	1	29	29	29	29	29.0	39.04
18	1	27	27	28	28	27.5	39.11
19	1	29	29	28.5	28	28.6	42.14
20	1	29	29	29	29	29.0	40.48
21	\rightarrow	26	26	26	26	26.0	39.16
22	\rightarrow	26	26	26	26	26.0	39.60
23*	\rightarrow	28	28	27	27	27.5	39.70
24	\rightarrow	28.5	28.5	27	27	27.8	40.25
25	\rightarrow	28	28	28	28	28.0	40.77
26	\rightarrow	27	27	29	29	28.0	39.14
27*	\rightarrow	28	28	28	28	28.0	38.58
28	\rightarrow	27	27	27	27	27.0	38.64
29	\rightarrow	27	27	27	27	27.0	39.56
30	\rightarrow	28	28	28	28	28.0	42.62
* Samples attair	ned rupture during	a E test					

Item	Position	11	12	13	14	la	f _c (MPa)
31	Ļ	23	23	23	23	23.0	38.06
32	Ļ	23	23	23	23	23.0	41.85
33	Ļ	23	23	23	23	23.0	38.55
34	\downarrow	24	24	24	24	24.0	38.86
35	Ļ	24	24	24	24	24.0	39.13
36	Ļ	24	24	24	24	24.0	38.94
37	Ļ	25	25	25	25	25.0	38.82
38	Ļ	25.5	25.5	25.5	25.5	25.5	39.05
39	Ļ	26	26	24	24	25.0	39.44
40	Ļ	24	24	24	24	24.0	42.08
41	↑ (29	29	29	29	29.0	43.06
42	↑ (29	29	29	29	29.0	39.38
43	↑ (29	29	29	29	29.0	41.80
44	↑ (28	28	28	28	28.0	38.55
45	↑	28	28	28	28	28.0	38.55
46	↑ (28	28	28	28	28.0	38.91
47	↑ (28	28	27	27	27.5	38.48
48	↑	27	28	28	27	27.5	39.55
49	↑ (27	27	27	27	27.0	40.41
50	↑ (27	27	27	27	27.0	38.46
51	\rightarrow	26	26	26	26	26.0	41.47
52	\rightarrow	26	26	26	26	26.0	42.59
53	\rightarrow	26	26	26	26	26.0	38.90
54	\rightarrow	26	26	26	26	26.0	38.63
55	\rightarrow	26	26	26	26	26.0	39.20
56	\rightarrow	28	28	27	27	27.5	39.13
57	\rightarrow	28	27.5	27.5	27.5	27.6	40.91
58	\rightarrow	28	28	28	28	28.0	38.73
59	\rightarrow	28	28	28	28	28.0	40.41
60	· · · ·	28	28	28	28	28.0	10.54

Table 16Experimental data obtained for C40 concrete samples - Set 2

Item	Position	11	12	13	14	la	f _c (MPa)
61	\downarrow	24	24	24	24	24.0	39.13
62	\downarrow	24	24	24	24	24.0	38.62
63	\downarrow	24	24	24	24	24.0	39.43
64	\downarrow	24	24	24	24	24.0	40.21
65	\downarrow	24	24	23	23	23.5	42.91
66	Ļ	24	23.5	23.5	23.5	23.6	38.29
67	Ļ	23.5	23.5	23.5	24	23.6	39.20
68	Ļ	25	25	25	25	25.0	38.46
69	Ļ	25	25	25	25	25.0	38.81
70	Ļ	24	24	24	24	24.0	41.67
71	↑	29	29	29	29	29.0	38.82
72	1	29	29	29	29	29.0	38.90
73	↑	29	29	29	29	29.0	38.76
74	↑	29	29	29	29	29.0	38.58
75	↑	31	31	31	31	31.0	40.20
76	↑	31	31	29	29	30.0	41.65
77	↑ (27	27	27	27	27.0	38.78
78	↑	26	26	26	26	26.0	38.31
79	↑	26	26	26	26	26.0	43.21
80	↑	26	26	26	26	26.0	39.99
81	\rightarrow	28	28	26	26	27.0	39.20
82	\rightarrow	27	27	27	27	27.0	42.74
83	\rightarrow	27	27	27	27	27.0	40.59
84	\rightarrow	29	29	29	29	29.0	43.11
85	\rightarrow	28	28	28	28	28.0	42.07
86	\rightarrow	28	28	28	28	28.0	39.22
87	\rightarrow	28	28	28	28	28.0	38.39
88	\rightarrow	29	29	29	29	29.0	40.29
89	\rightarrow	29	29	29	29	29.0	41.13
90	→	26	26	26	26	26.0	42.70

Table 17Experimental data obtained for 40 concrete samples – Set 3

Experimental data obtained for C45 concrete samples - Set 1

Item	Position	11	12	13	14	la	f _c (MPa)
1*	\downarrow	28	28	28	28	28.0	44.69
2	\downarrow	28	28	28	28	28.0	44.67
3	\downarrow	29	29	29	29	29.0	45.16
4	\downarrow	29	29	29	29	29.0	45.10
5	\downarrow	29	29	29	29	29.0	45.31
6	\downarrow	31	31	31	31	31.0	46.42
7	\downarrow	31	31	31	31	31.0	46.84
8	Ļ	31	31	31	31	31.0	44.81
9	Ļ	31	31	29	29	30.0	44.56
10	Ļ	30	30	30	30	30.0	45.59
11	<u>↑</u>	32	32	32	32	32.0	48.32
12	<u>↑</u>	32	31.5	32	15**	31.8	43.57
13	<u>↑</u>	31.5	31.5	32	31.5	31.6	45.45
14*	<u>↑</u>	32	32	32	32	32.0	47.58
15	↑	33	33	33	33	33.0	46.54
16	↑	33	33	33	33	33.0	46.19
17	1	33	33	33	33	33.0	42.79
18	1	34	34	34	34	34.0	43.23
19	1	34	34	33.5	33.5	33.8	42.53
20	1	34	34	34	34	34.0	44.58
21	\rightarrow	31	31	31	31	31.0	45.06
22	\rightarrow	31	31	31	31	31.0	47.99
23*	\rightarrow	31	31	31	31	31.0	48.00
24	\rightarrow	32	32	32	32	32.0	45.58
25	\rightarrow	32	32	32	32	32.0	48.79
26	\rightarrow	32	32	32	32	32.0	43.00
27*	\rightarrow	33	33	33	33	33.0	45.42
28	\rightarrow	33.5	33.5	32	32.5	32.9	44.64
29	\rightarrow	33	33	32.5	32.5	32.8	45.54
30	\rightarrow	32	32	32	32	32.0	43.99
* Samples attair	ned rupture during	g E test, ** Discarde	ed values				

Experimental data obtained for C45 concrete samples - Set 2

Item	Position	11	12	13	14	la	f _c (MPa)
31	Ļ	30	30	30	30	30.0	47.44
32	Ļ	30	30	30	30	30.0	46.43
33	Ļ	30	30	30	30	30.0	44.63
34	\downarrow	30	30	30	30	30.0	44.58
35	\downarrow	30	30	30	30	30.0	45.82
36	\downarrow	30	30	28	28	29.0	46.57
37	\downarrow	29	29	29	29	29.0	45.61
38	\downarrow	29	29	29	29	29.0	44.95
39	\downarrow	31	31	31	31	31.0	47.76
40	\downarrow	31.5	32	32	31.5	31.8	46.72
41	1	32	32	32	32	32.0	47.86
42	1	33	33	33	33	33.0	44.79
43	↑	33	33	33	33	33.0	46.69
44	↑	33	33	33	33	33.0	45.16
45	1	34	34	34	34	34.0	44.42
46	1	32	32	32	32	32.0	43.49
47	1	32	32	32	32	32.0	48.04
48	1	34	34	34	34	34.0	45.51
49	1	34	34	34	34	34.0	46.92
50	1	34	32	34	32	33.0	47.84
51	\rightarrow	32	32	32	32	32.0	45.39
52	\rightarrow	32	32	32	32	32.0	48.46
53	\rightarrow	32	32	32	32	32.0	45.80
54	\rightarrow	32	32	32	32	32.0	45.02
55	\rightarrow	32	32	32	32	32.0	46.75
56	\rightarrow	33	33	32.5	32.5	32.8	45.39
57	\rightarrow	33	33	33	32.5	32.9	45.52
58	\rightarrow	31	31	32	32	31.5	48.24
59	\rightarrow	31	31	31.5	31.5	31.3	46.23
60	\rightarrow	31	31	31	31	31.0	47.48

Experimental data obtained for C45 concrete samples - Set 3

Item	Position	11	12	13	14	la	f _c (MPa)
61	\downarrow	30	30	30	30	30.0	45.16
62	Ļ	30	30	30	30	30.0	45.25
63	\downarrow	30	30	30	30	30.0	44.59
64	\downarrow	29	29	29	29	29.0	45.79
65	Ļ	29	29	29	29	29.0	46.37
66	Ļ	29	29	29	29	29.0	48.17
67	Ļ	29	29	29	29	29.0	47.53
68	Ļ	31	31	30.5	30.5	30.8	45.45
69	Ļ	31	30.5	30.5	30.5	30.6	48.27
70	Ļ	31	31	31	31	31.0	45.99
71	1	33	33	33	33	33.0	47.20
72	1	33	33	33	33	33.0	45.23
73	↑ (33	33	33	33	33.0	46.96
74	↑	33	33	33	33	33.0	45.28
75	1	33	33	33	33	33.0	45.58
76	1	33	33	31	31	32.0	43.93
77	1	32	32	32	32	32.0	42.36
78	1	33	33	33	33	33.0	44.73
79	1	33	33	33	33	33.0	46.40
80	1	32	32	32	32	32.0	42.88
81	\rightarrow	32	32	32	32	32.0	45.07
82	\rightarrow	32	32	32	32	32.0	46.68
83	\rightarrow	30	30	30	30	30.0	45.86
84	\rightarrow	30	30	30	30	30.0	45.28
85	\rightarrow	30	30	30	30	30.0	45.62
86	\rightarrow	30	30	30	30	30.0	47.25
87	\rightarrow	32	32	33	33	32.5	47.16
88	\rightarrow	33	33	33	33	33.0	47.66
89	\rightarrow	33	33	33	33	33.0	45.70
90	\rightarrow	33	33	33	33	33.0	45.20

Experimental data obtained for C50 concrete samples - Set 1

Item	Position	11	12	13	14	la	f _c (MPa)
1	\downarrow	32	32	32	32	32.0	50.87
2	\downarrow	32	32	32	32	32.0	47.30
3	\downarrow	32	32	32	32	32.0	48.55
4	\downarrow	32	32	32	32	32.0	49.19
5	\downarrow	32	32	30	30	31.0	49.21
6	\downarrow	30	30	30	30	30.0	56.84
7*	\downarrow	33	33	33	33	33.0	54.77
8	\downarrow	33	33	33	33	33.0	47.57
9	\downarrow	32	32	32	32	32.0	55.41
10	\downarrow	33	33	31	31	32.0	53.34
11	1	35	35	35	35	35.0	47.57
12	1	33	33	33	33	33.0	54.79
13*	1	35	35	35	35	35.0	54.81
14	1	35	35	33	33	34.0	48.73
15	1	36	36	36	36	36.0	48.13
16	1	36	36	36	36	36.0	48.78
17*	1	35	35	35	35	35.0	33.50
18	1	34	34	34	34	34.0	50.57
19	1	36	36	34	34	35.0	48.47
20	1	35	35	35	35	35.0	49.31
21	\rightarrow	33	33	33	33	33.0	47.47
22	\rightarrow	33	33	33	33	33.0	49.25
23*	\rightarrow	34	34	32	32	33.0	53.86
24	\rightarrow	34	34	34	34	34.0	53.65
25	\rightarrow	32	32	32	32	32.0	50.03
26	\rightarrow	34	34	34	34	34.0	49.20
27*	\rightarrow	24	24	22	22	23.0	31.28
28	\rightarrow	31	31	31	31	31.0	43.02
29	\rightarrow	33	33	31	31	32.0	41.97
30	\rightarrow	31	31	31	31	31.0	47.36
* Samples attair	ned rupture during	a E test					

Experimental data obtained for C50 concrete samples - Set 2

Item	Position	11	12	13	14	la	f _c (MPa)
31	\downarrow	33	33	33	33	33.0	55.88
32	\downarrow	33	33	33	33	33.0	51.66
33	\downarrow	33	33	31	31	32.0	48.87
34	\downarrow	31	31	31	31	31.0	54.57
35	Ļ	32	32	32	32	32.0	51.26
36	\downarrow	32	32	32	32	32.0	56.26
37	\downarrow	32	32	32	32	32.0	48.52
38	\downarrow	31	31	31	31	31.0	56.93
39	\downarrow	33	33	33	33	33.0	52.01
40	\downarrow	33	31	33	31	32.0	55.72
41	1	34	34	34	34	34.0	50.88
42	1	34	34	34	34	34.0	48.92
43	1	34	34	34	34	34.0	48.19
44	1	34	34	34	34	34.0	52.48
45	1	34	34	36	36	35.0	48.70
46	1	36	36	36	36	36.0	47.43
47	1	36	36	36	36	36.0	49.90
48	1	35	35	35	35	35.0	48.43
49	1	36	36	36	36	36.0	51.80
50	1	35	35	35	35	35.0	53.87
51	\rightarrow	33	33	33	33	33.0	51.11
52	\rightarrow	33	33	33	33	33.0	48.10
53	\rightarrow	33	33	33	33	33.0	48.66
54	\rightarrow	34	34	34	34	34.0	48.70
55	\rightarrow	34	34	34	34	34.0	55.28
56	\rightarrow	34	34	34	34	34.0	55.74
57	\rightarrow	32	32	32	32	32.0	48.69
58	\rightarrow	34	34	33.5	33.5	33.8	47.95
59	\rightarrow	34	33.5	33.5	33.5	33.6	55.79
60	\rightarrow	33	33	33	33	33.0	54.57
* * Discarded vo	alue						

Experimental data obtained for C50 concrete samples - Set 3

Item	Position	11	12	13	14	la	f _c (MPa)
61	\downarrow	31	31	31	31	31.0	49.20
62	\downarrow	31	31	31	31	31.0	49.50
63	\downarrow	32	32	32	32	32.0	47.35
64	Ļ	32	32	32	32	32.0	50.87
65	Ļ	32	32	32	32	32.0	47.64
66	Ļ	32	32	32	32	32.0	48.41
67	\downarrow	34	34	32	32	33.0	51.86
68	\downarrow	34	34	34	34	34.0	49.40
69	Ļ	34	32	34	32	33.0	50.67
70	Ļ	33	33	33	33	33.0	47.47
71	↑ (36	36	34	34	35.0	49.07
72	↑	36	36	36	36	36.0	47.52
73	↑	35	35	35	35	35.0	50.23
74	↑	36	36	36	36	36.0	51.32
75	↑	36	36	36	36	36.0	54.05
76	↑	37	37	37	22**	37.0	52.13
77	↑	34	34	34	34	34.0	51.34
78	↑	33	33	33	33	33.0	49.10
79	↑ (35	35	35	35	35.0	51.26
80	↑ (36	34	36	34	35.0	56.99
81	\rightarrow	33	33	33	33	33.0	49.82
82	\rightarrow	33	33	33	33	33.0	57.92
83	\rightarrow	33	33	34	34	33.5	53.54
84	\rightarrow	33	33	31	31	32.0	46.01
85	\rightarrow	31	31	31	31	31.0	46.00
86	\rightarrow	34	34	34	34	34.0	47.67
87	\rightarrow	34	34	34	34	34.0	47.67
88	\rightarrow	33	33	33	33	33.0	50.51
89	\rightarrow	34	32	34	32	33.0	50.10
90	\rightarrow	33	33	32	32	32.5	47.26
* * Discarded v	alue						



Figure 5

Boxplots for the 3 sets of points grouped according to the shot position

Table 24

Coefficients of the linear regression models on the form $f_c = al+b$ as a function of each shot position

Position	a	b	MSE	R	р
2↓	1.6045	-1.4504	0.0335	0.968	0
1 →	1.5403	-2.1899	0.0305	0.973	0
3↑	1.5887	-6.1778	0.0299	0.976	0



Figure 6

Comparison of the linear regression models adopted for each shot position





Comparison between values obtained via sclerometer (f_{cs}) and mechanical tests (f_c) obtained in a construction site

Figure 8 shows the Two-sided Kolmogorov-Smirnov test (KS-test) for all samples. Each entry shows the p-value for the KS-test, where p-values leastest than 0.05 indicates that the samples are drawn from the same continuous distribution. The Two-sided Kolmogorov-Smirnov tests whether two data samples come from the same distribution. The KS-test has the advantage of making no assumption about the distribution of data (nonparametric and distribution free). The null hypothesis is the two samples come from a common distribution and it is rejected when the associated p-values are greater than 0.05. A total of 210 pairs were compared, and according to the tests, five pairs of samples were drawn from the same distribution: $(C25\rightarrow)/(C25\downarrow)$, $(C25\uparrow/C35\downarrow)$, $(C30\rightarrow/C35\downarrow)$, $(C45\rightarrow/C50\downarrow)$, $(C45\uparrow/C50\rightarrow)$,

and the results involving these pairs of data sets shall be carefully analyzed considering the statistical interplay between the groups.

3.2 Evaluation of concrete structural members

Based on the data analysis (Botelho et al [11]), an in situ experiment was accomplished on concrete members during construction. The methodology consisted of comparing the fc evaluated via sclerometer measurements, employing the correlation curves proposed in this study. with the fc values obtained from mechanical tests on concrete specimens molded for technological control. The following steps were performed:



Figure 8

Two-sided Komolgorov-Smirnov test (KS-test) for all samples. Each entry shows the p-values for the KS-test, where p-values leastest than 0.05 indicates that the samples are dram from the same continuous distribution

Analysis and validation of correlation curves between sclerometry and compression tests for the evaluation of compressive strength of concretes

- 48 in situ measurements via sclerometer on concrete elements (columns, beams, slabs and foundation blocks) were performed 28 days after casting;
- the corresponding compressive strength f_{cs} was evaluated via Equations [1], [2] or [3]. employing the a and b coefficients

(see Table 4) according to the employed shot direction: Position 1 (\rightarrow): $f_{cs} = 1.5403$ Ia - 2.1899

(1)

(2)

Position 2 (\downarrow): $f_{cs} = 1.6045 \text{ Ia} - 1.4504$

Table 25

Comparison between sclerometer and mechanical tests performed in a construction site

Item	Structural member	Shot direction	I	fc s (MPa)	fc (MPa)	fc / fc s
1	column	\rightarrow	35.08	51.84	34.80	1.49
2	column	\rightarrow	36.06	53.35	34.80	1.53
3	column	\rightarrow	35.38	52.31	34.80	1.50
4	column	\rightarrow	34.82	51.44	29.70	1.73
5	column	\rightarrow	34.70	51.26	29.70	1.73
6	column	\rightarrow	33.99	50.16	25.00	2.01
7	column	\rightarrow	34.88	51.54	29.70	1.74
8	column	\rightarrow	35.44	52.40	29.70	1.76
9	column	\rightarrow	34.86	51.50	30.00	1.72
10	column	\rightarrow	34.75	51.34	30.00	1.71
11	slab	↑	37.20	52.92	33.00	1.60
12	slab	↑	35.79	50.68	25.00	2.03
13	slab	↑	36.76	52.22	28.20	1.85
14	slab	↑	37.42	53.27	35.00	1.52
15	slab	↑	37.76	53.81	37.20	1.45
16	column	\rightarrow	35.12	51.91	30.00	1.73
17	column	\rightarrow	34.90	51.57	30.00	1.72
18	column	\rightarrow	36.09	53.40	34.80	1.53
19	column	\rightarrow	35.03	51.77	34.80	1.49
20	column	\rightarrow	35.81	52.97	30.00	1.77
21	column	\rightarrow	34.55	51.03	30.00	1.70
22	column	\rightarrow	34.45	50.87	30.00	1.70
23	column	\rightarrow	35.31	52.20	34.80	1.50
24	column	\rightarrow	35.63	52.69	34.80	1.51
25	column	\rightarrow	35.41	52.35	34.80	1.50
26	column	\rightarrow	35.48	52.46	30.00	1.75
27	column	\rightarrow	35.18	52.00	30.00	1.73
28	column	\rightarrow	35.34	52.24	30.00	1.74
29	column	\rightarrow	34.85	51.49	30.00	1.72
30	column	\rightarrow	27.56	40.26	22.10	1.82
31	column	\rightarrow	28.07	41.05	24.50	1.68
32	column	\rightarrow	33.88	50.00	24.50	2.04
33	column	\rightarrow	30.11	44.19	23.80	1.86
34	column	\rightarrow	31.41	46.19	23.80	1.94
35	column	\rightarrow	30.02	44.05	24.50	1.80
36	column	\rightarrow	32.60	48.02	23.80	2.02
37	beam	→	33.55	49.49	23.80	2.08
38	beam	\rightarrow	30.19	44.31	24.50	1.81
39	beam	\rightarrow	33.25	49.03	24.50	2.00
40	beam	\rightarrow	31.25	45.94	25.00	1.84
41	beam	\rightarrow	34.61	51.12	30.00	1.70
42	block	↓ ↓	29.29	45.55	25.00	1.52
43	block	↓	28.54	44.34	25.00	1.77
44	block	↓	29.10	45.24	25.00	1.81
45	slab*	↓	32.42	50.57	28.00	2.02
46	slab*	↓	32.80	51.18	31.00	1.83
4/	slab*	↓ ↓	33.86	52.88	31.00	
48	slab*	↓	32.46	50.63	28.00	1.63

Position 3 (
$$\uparrow$$
): $f_{rr} = 1.5887 \text{ Ia} - 6.1778$ (3)

where Ia is the average for 16 sclerometer readings, as specified by codes.

 f_{cs} values were compared with fc obtained from 28 days old cylindrical concrete samples, cast for technological control purposes.

3.3 Results

In spite of the high R values of the three adopted correlation curves, given by Equations 1-3, which denote a quite good correlation with the experimental database, *in situ* measurements generated rather

discrepant values for the compressive strength of the material in study. As one can see in Table 25, f_{cs}/f_c ratios range from 45% to 108%. This pattern may be clearly observed in Figure 7, where $f_c x f_{cs}$ points are plotted along with a bisector line. An aspect that deserves attention is the fact that the adopted correlation curves are against safety, by taking the f_c values measured on concrete samples via mechanical tests as a reference.

Table 26 shows the correlation coefficients for the models presented in this paper. The results for slab (vertical shot position) member present higher correlation values whereas a moderated correlation can be observed for slab (downward position) and for column members. Poor correlations were obtained for beam

Table 26

Correlation coefficients for each member and position. The number of samples is shown in the third column

Position	Member	N° samples	Corr. coefficient
\rightarrow	beam	5	0.543865
\downarrow	block	3	-
\rightarrow	column	31	0.789565
↑	slab	5	0.971064
Ļ	slab*	4	0.764660



Figure 9

Compressive strength values: experimental (f_{c}) and estimated (f_{cs}) according to shot direction for structural members beam, block and slab



Figure 10

Compressive strength values: experimental (f_c) and estimated (f_{cs}) according to shot direction for structural member column

member in the horizontal shot position. For the block member, it was not allowed to calculate the correlations due to the small number of samples available. One can observe moderate and higher correlation coefficients for some members, however a proper analysis involves considering the error when using the expressions given in Equations 1, 2 and 3.

Figures 9 and 10 show the experimental (f_c) and estimated (f_{cs}) compressive strength values according to shot direction for structural members beam, block, column and slab. The estimated values were obtained using Equations 1, 2 and 3 depending on the position of the sclerometer. Percentage dif-



Figure 11

Percentage difference between experimental (f_{c}) and estimated (f_{cs}) compressive strength according to shot direction for structural member

ferences between experimental (f_c) and estimated (f_{cs}) compressive strength are shown in Figure 11. As can be seen in this figure, there are an overestimation of the compressive strength which in extreme cases may reach 100%. Several factors such as humidity, carbonatization, chemical aggressions, microcracks and history of the concrete influence the sclerometric index value. The concrete is permeable and the carbon dioxide may react with the substances in the concrete leading to the phenomenon of carbonatization. Cracking allows the penetration of water and carbon dioxide oxidating the armature. An interesting study is establishing a correction factor of the readings obtained take into consideration the carbonatization phenomenon by comparing the sclerometric test results conducted on carbonatated and non-carbonatated specimens. The analysis conducted in this paper denotes the need for more careful evaluation of the protocols concerning the application of sclerometry on real life situations. The authors consider that it is paramount to establish a careful methodology for obtaining adequate correlation curves, as well as the definition of calibration procedures aiming the generalization of the technic to the wide variety of concretes and scenarios in the construction industry.

4. Conclusions

In spite of the fact that the application of sclerometry is increasing all over the world, due to its feasibility and non-destructive characteristics, it is paramount to establish protocols that allow adequate correlation curves. The experimental results presented herein denote the necessity of specific codes for the safe application of this technique in practical applications. To this end, it is necessary to perform further experimental investigations. This study is a preliminary step to a broader research aiming to contribute to improvements of the Brazilian code NBR 7584:2012 (ABNT [8]).

5. Acknowledgements

The authors acknowledge the financial support from: Fundação de Amparo à Pesquisa de Minas Gerais – FAPEMIG. Conselho Nacional de Desenvolvimento Científico e Tecnológico – CNPq. Coordenação de Aperfeiçoamento de Pessoal de Nível Superior – CAPES and Pró-Reitoria de Pós-Graduação e Pesquisa da Universidade Federal de Juiz de Fora – PROPP/UFJF.

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