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## Analysis of instability of tall buildings with prestressed and waffle slabs

# Análise da instabilidade de edifícios altos com lajes protendidas e lajes nervuradas

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#### **Abstract**

The construction system of prestressed flat slabs has been gaining market in Brazil, since it eliminates the use of beams, allows you to perform structures under coluns by area and reduces the cycle of concrete slabs. Thus the analysis of global stability of buildings, takes into account the effects of 2nd order, and these additional effects to the structure obtained from the deformation thereof, calculated by the iterative method P-Delta. The Brazilian ABNT NBR 6118: 2014 [2] assesses the overall stability of reinforced concrete structures through practical parameters, which are the parameter  $\alpha$  (Alpha) and  $\gamma_z$  (Gamma z) coefficient. In this research we seek to study the global stability of slender buildings consist of flat slabs, with slenderness (ratio of the smaller width with the height of the building) approximately one to six, from the modeling of a building with prestressed slabs nonadherent and waffle slabs. To model will use the commercial software CAD / TQS.

Keywords: global stability, analysis of 2nd order, gamma z, p-delta.

### Resumo

O sistema construtivo de lajes planas protendidas vem ganhando mercado no Brasil, pois dispensa o uso de vigas, permite executar estruturas com menos pilares por área e reduz o ciclo de concretagem das lajes. Assim a análise de estabilidade global de edificações, leva em consideração os efeitos de 2ª ordem, sendo estes efeitos adicionais à estrutura obtidos a partir das deformações da mesma, calculadas pelo método iterativo P-Delta. A norma brasileira ABNT NBR 6118:2014 [2] avalia a estabilidade global de estruturas de concreto armado através de parâmetros práticos, sendo estes o parâmetro α (alfa) e o coeficiente γ<sub>z</sub> (gama z). Nesta pesquisa busca-se estudar a estabilidade global de edificações esbeltas compostas por lajes planas, com ordem de esbeltez (relação da menor largura com a altura da edificação) de um para seis, a partir da modelagem de uma edificação com lajes protendidas não-aderentes e lajes nervuradas. Para modelagem será utilizado o programa comercial CAD/TQS.

Palavras-chave: estabilidade global, análise de 2ª ordem, gama z, p-delta.

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#### 1. Introduction

Of the slab construction technologies that are used in the Brazilian market, prestressed flat and waffle slabs stand out for providing increased productivity and material savings compared to conventional slab and beam systems. Moreover, these slabs allow for larger spans, fewer formworks, better utilization of materials, and greater architectural flexibility.

Because of these advantages, a feasibility analysis of tall and slender buildings that use these types of construction systems is proposed in terms of the global stability of the structure.

The bracing in these types of buildings relies on the group of columns that are part of the buildings. Because the structure is devoid of beams, there is no a priori stabilization of the building by space frames.

In this case, it is common to use conveniently positioned "U" or "L" shaped column-walls to ensure the required stiffness in both directions for stability. Prestressed slabs have a minimum thickness of sixteen centimeters (Item 13.2.4.1 of ABNT NBR 6118:2014 [2]), but it is common to use thicknesses of at least eighteen centimeters to ensure the stiff diaphragm effect and the bracing of columns, which guarantee that all of the components work together to stabilize the structure. The greater thickness in the region where the waffle slabs connect to the columns makes this location sufficiently stiff to stabilize the building.

This study evaluates the influence of variations in several parameters on the global stability of the proposed structure, including the slab thickness, the column section, the coefficients that represent the physical nonlinearity of the structural elements, the height of the typical floor plan and the characteristic strength of the concrete.

#### 1.1 Objectives

The aim of this research is to analyze different models for buildings with slenderness ratios of one to six by varying the type of slab construction system that is used between prestressed slabs and waffle slabs. Thus, this study will evaluate the instability parameters of the structure that result from variations of several general parameters, such as the thickness of the slabs, the sections of the columns, the coefficients that represent the physical nonlinearity of structural elements, the height of the typical floor plan and the characteristic strength of the concrete.

The commercial software CAD/TQS version 17.11.8 is used to analyze and test these instability parameters.

#### Literature review

#### 2.1 Nonlinear analysis

Reinforced concrete structures display important nonlinear behavior, which is a result of the nonlinear relationships between the forces and displacements that result from physical and geometric nonlinearities. Such behavior is inherent in all reinforced concrete structures and must be taken into account during structural analyses.

The physical nonlinearity of reinforced concrete is generated because it consists of materials with different physical properties that create an anisotropic, heterogeneous material with an elastic modulus that varies at each point of the stress-strain diagram curve. In addition, the difference between the compressive strength and tensile strength of concrete is large. In applications, this difference leads to the formation of cracks by tension, which reduces the bearing capacity of the parts. In addition to cracking, creep, the combination of different forces, and the presence of rebar also generate nonlinear behavior in the concrete.

ABNT NBR 6118:2014 [2] uses a simplification to consider this physical nonlinearity. The stiffnesses of the structural elements are modified using reduction coefficients for each type of element (beams, columns and slabs) according to the influence that the element has on the global stability of the structure. A stiffness that is reduced by a coefficient is called the effective stiffness or the secant stiffness.

The aforementioned standard requires the physical nonlinearity to be considered and proposes values that should be adopted to reduce the stiffnesses of the structural elements, namely:

- Slabs: (EI)<sub>sec</sub>= 0,3 E<sub>ci</sub>I<sub>c</sub>
- Beams:

where:

I: moment of inertia of the gross concrete section;

E<sub>a</sub>: modulus of the initial tangential strain of the concrete.

Item 15.7.3 of the previous version of the standard, ABNT NBR 6118:2007 [1], states that if the global instability factor  $\gamma_z$  is less than 1.3 and the bracing structure of the building is only composed of columns and beams, the effective or secant stiffness of the columns and beams could be taken as:

Columns and Beams: (EI)<sub>sec</sub>= 0,7 E<sub>cl</sub>I<sub>c</sub>

However, this consideration is not included in the new 2014 version. Less cracking occurs in prestressed elements (slabs and beams) than in reinforced concrete elements. Thus, it would be interesting to study the use of reduction coefficients with higher values than those indicated by the current standard, or retaining the values from the previous version of the standard and the value of 0.7 for a prestressed slab, when a slab is used to resist the horizontal forces; i.e., when it is part of the global bracing system of the structure.

Even if a structure is built with a material that has a linear stressstrain relationship, it may exhibit nonlinear behavior when it experiences major displacements. The lateral strain of a structural component leads to the appearance of additional bending moments (second-order moments) due to the new location of the vertical force. This behavior is called geometric nonlinearity because it lacks a linear relationship between the forces and effects.

To perform a structural analysis that considers geometric nonlinearity, ABNT NBR 6118:2014 [2] uses a safety formula for the combination of actions. The actions are increased by the factor g/g<sub>ra</sub>, and the internal forces are then increased by the factor  $g_{\rm fs}$ , which is equal to 1.1.

#### 2.2 Second-order effects

The first-order structural analysis considers the structure in its undisturbed geometric configuration. When the deformed geometry of the structure is considered, additional forces, which are called second-order effects, are generated in the structural system; these

additional effects on the structure are caused by its deformation and are responsible for the nonlinear behavior of the structure. One way to take into consideration this effect in the structure is the use of Iterative Method P-Delta (P- $\Delta$ ).

The iterative P-Delta method, which converts the lateral displacement into equivalent horizontal forces, is used in the second-order analysis of structures. The first-order analysis of a structure, which considers its undisturbed initial configuration, obtains the displacements, which will be the basis for the definition of "pseudo" horizontal loads that are equivalent to the second-order loading. In each step, new "pseudo" lateral forces are obtained, which tend to decrease as the structure reaches an equilibrium position. The iterations end when the effect of the "pseudo" load is small compared to the effect of the previous load or when is determined that the structure will cannot have global stability.

#### 2.3 Global stability

The global stability of the structure is defined as its sensitivity to second-order effects and is an inversely proportional relationship in which the more sensitive the structure is to the second-order effects, the less stable it will be.

The Brazilian standard ABNT NBR 6118:2014 [2] does not require second-order forces to be considered if they are less than 10% of the first-order forces. Thus, it is always necessary to perform the second-order analysis regardless of whether these effects will be

used to design the structure. The standard uses the gamma Z ( $\gamma_z$ ) coefficient and the alpha ( $\alpha$ ) parameter to assist in the decision to consider the second-order effects.

The  $\gamma_z$  instability coefficient was introduced by Franco and Vasconcelos (1991) [5] and measures the sensitivity of the structure to second-order effects; it can also be used to increase the first-order effects from the horizontal loads to obtain the approximate second-order effects. The  $\gamma_z$  coefficient is defined by:

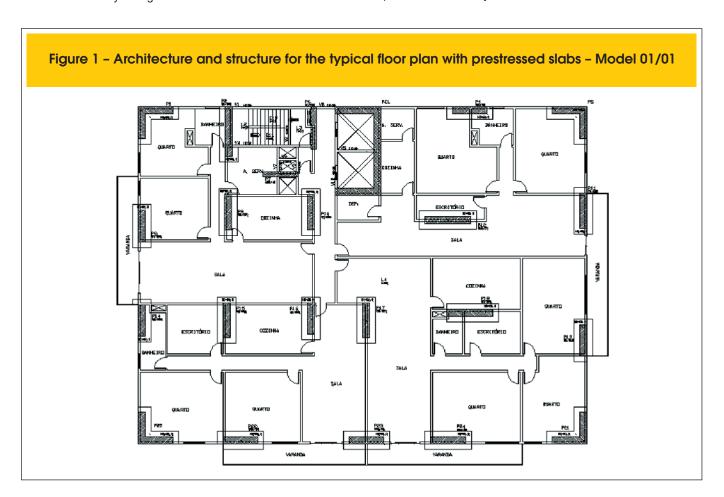
$$\gamma_z = \frac{1}{1 - \frac{nM_d}{M_{1d}} * \frac{1}{1,1}}$$
 (1)

where:

 $\Delta M_{\rm d}$ : The sum of the products of all of the vertical forces that act on the structure by the horizontal displacements, which are obtained in the first-order analysis:

 $\rm M_{1d}$ : The moment of tipping, which is the sum of the moments that are produced by the horizontal forces with respect to the base of the structure.

Feitosa e Alves (2014) [6] presents a study on the global instability of buildings with slenderness ratios of one to four with flat slabs. In this study it is presented the influence of the nonlinearity effect and impact on the instability coefficient.



#### 2.4 Main factors that influence the global stability

Of the factors that influence the global stability of buildings, the vertical loading and the stiffness of the structure are the most influential. The  $\gamma_z$  parameter indicates this relevance in the formula because an increase in the vertical load increases the value of  $\gamma_z$  for the same horizontal loading. A greater horizontal loading does not increase the value of  $\gamma_z$  because the first- and second-order forces increase at the same rate; that is,  $\Delta M_{\rm d}$  /  $M_{\rm 1d}$  remains constant. The stiffer the structure is, the smaller its displacements will be; this will generate lower second-order moments, which will reduce the  $\gamma_z$  coefficient.

### 3. Models

The building models feature prestressed flat slabs or waffle slabs. Slenderness ratios of one to six were adopted, thus, a building width of 24 meters, which is measured from the edge of the corner column, gives a building height of 144 meters. This slenderness ratio includes the tower geometry but does not include the base of the building model. Based on an architectural plan with a geometrically-asymmetric design, the buildings were modelled using the CAD/TQS software to evaluate the influence of the parameters based on the  $\gamma_z$  instability parameter and lateral displacements.

### 3.1 Analysis model VI - CAD/TQS

Model VI simulates the building as a single frame that is composed of elements that simulate the slabs, beams and columns of the structure. The slabs contribute strength to resist wind forces along with the beams and columns. The connections between the beams and columns are regarded as semi-rigid.

#### 3.2 Considering P-Delta in CAD/TQS

TQS Informática LTDA developed a coefficient called RM2M1 to represent the intensity of the second-order forces relative to the first-order forces. The second-order forces are calculated using the iterative P-Delta method. RM2M1 is given by:

$$RM2M1 = 1 + \frac{M_2}{M_1}$$
 (2)

where:

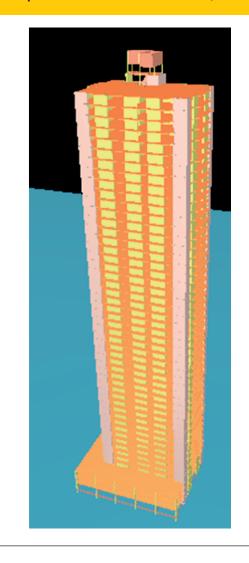
 $\mathrm{M}_{1}$ : The moment of the horizontal forces with respect to the base of the building:

 ${
m M_2}$ : The sum of the vertical forces multiplied by the displacement of the nodes of the structure due to the nonlinear combination of horizontal forces from the P-Delta calculation.

### 3.3 Description of models

The building shown in Figure 1 was modelled with a flat slab, and the cross section of the columns was varied until it reached a value similar to the  $\gamma_z$  coefficient limit that is recommended by ABNT NBR 6118:2014 [2]. This model, which is called 01/01, was the basis for

Figure 2 – 3D – Typical floor plan with prestressed slabs – Model 01/01

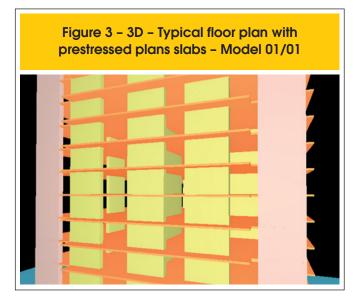


the subsequent models and resulted in a value of  $\gamma_z$  of 1.297 (wind 90°-270°). The Figures 2 and 3 show 3D details of building.

In model 01/02, the thickness of the lift column (stiff core) was changed to assess whether a higher stiffness would lead to a significant reduction in the value of  $\gamma_z$ .

In model 01/03, the thickness of the slab was increased because in model VI takes into account the effect of the transverse bending stiffness of the slabs on the frame. Thus, the slabs begin to contribute to resisting the horizontal forces. Therefore, increasing the thickness of the slab would increase the stiffness of the bracing system. The increased weight due to the increased thickness of the slab would be offset by its increased stiffness, as stated FEITOSA and ALVES (2015) [6].

In model 01/04, the ceiling height of the typical floor plan was decreased, which increased the frame stiffness due to the decrease in the length of the unbraced columns.



As stated previously, prestressed slabs and beams experience less cracking than reinforced concrete slabs and beams. Thus, the values of the coefficients that represent the physical nonlinearity of these elements were increased in model 01/05.

Finally, model 01/06 considered all of the changes from the previous models to decrease the section of the columns and evaluate

the reduction of the amount of concrete used for the columns relative to the total amount of concrete used in the structure. The data for the model with the flat slabs are presented in Table 1.

The Model 02/01 is based on model 01/01, but the construction method was changed to waffle slabs as shown in Figures 4, 5 and 6. The formworks were sixteen centimeters high, and the cover was five centimeters thick. The cross section of the columns was varied, and the model resulted in a  $\gamma_z$  value of 1.297 (wind 90°-270°). The Figures 5 and 6 show 3D details of building.

The changes in models 02/02, 02/03 and 02/04 were the same as those that were made in the models with the prestressed slabs. The changes in the coefficients that represent the physical nonlinearity were not implemented because of the absence of prestressed elements in the waffle slab models.

In model 02/05, the cross sections of the columns were decreased as much as possible while keeping the  $\gamma_z$  coefficient below the limit that is recommended by the standard. The data for the waffle slab models are presented in Table 2.

## 4. Results and discussions

#### 4.1 Analysis results of models 01/01 to 01/06

The results obtained using the proposed design shown in Figure 1 and the models described above were analyzed and are shown in Tables 3, 4 and 5.

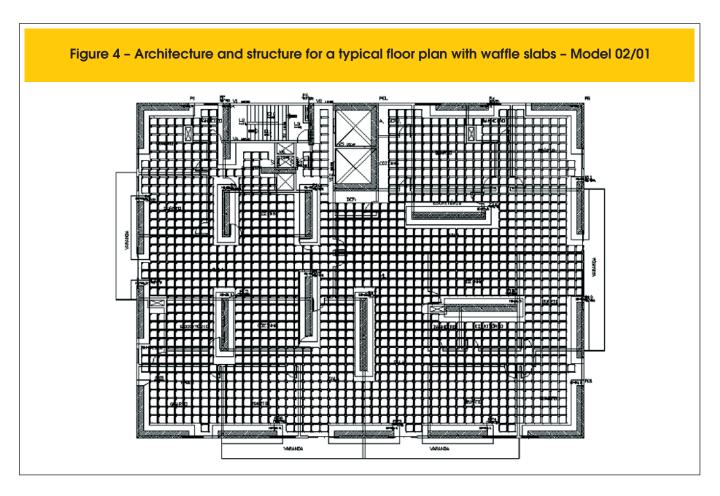


Figure 5 - 3D - Typical floor plan with waffle slabs - Model 02/01

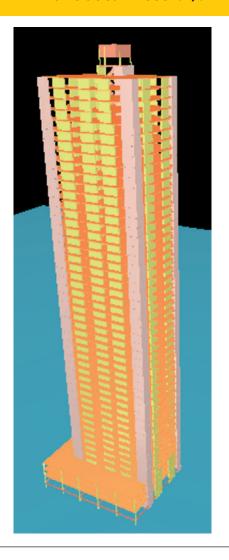


Figure 6 – 3D – Typical floor plan with details of waffle slabs –Model 02/01



Increasing the thickness of the lift column (stiff core) in model 01/02 did not cause a significant reduction in the  $\gamma_z$  coefficient; the reductions were approximately 0.617% (wind 90°-270°) and 0% (wind 0°-180°).

The increase in slab thickness that was considered in model 01/03 reduced the  $\gamma_z$  instability coefficient by approximately 4.472% (wind 90°-270°) and 4.111% (wind 0°-180°). These reductions demonstrate the importance of considering the cross stiffness of the slab in the global stability of the structure.

Reducing the ceiling height of the floors in model 01/04 reduced  $\gamma_z$  by approximately 2.005% (wind 90°-270°) and 2.213% (wind 0°-180°).

The greatest reduction in the  $\gamma_z$  instability coefficient was obtained in model 01/05, which considers the largest values of the physical nonlinearity coefficients; the reductions were approximately 9.368% with wind directions of 90°-270° and 8.142% with wind directions of 0°-180°. These results confirm the possibility of extending the prestressed slabs, which increase the coefficient of physical nonlinearity when they are used in the bracing system of the structure because of their cross stiffness.

In model 01/06, the sections of the columns were decreased while keeping the  $\gamma_z$  coefficient below the limit that is recommended by ABNT NBR 6118:2014 [2]. Compared with model 01/01, model 01/06 resulted in a reduction of approximately 37.5% in the volume of concrete used for the columns and a reduction of approximately 31.3% in the formworks used for the columns.

Table 1 - Data for the prestressed slab models

	Prestressed slab – data from models												
	Lift column	Nonlinearity coefficient		Slab thickness		f <sub>ck</sub> (MPa)		Ceiling height					
Model	thickness (cm)	Slabs	Slabs Beams (cm)	(cm)	Slabs	Beams	Columns	for typical floor plan (m)					
01/01	40	0,3	0,4	18	30	30	40	3,24					
01/02	50	0,3	0,4	18	30	30	40	3,24					
01/03	40	0,3	0,4	20	30	30	40	3,24					
01/04	40	0,3	0,4	18	30	30	40	2,88					
01/05	40	0,7	0,7	18	30	30	40	3,24					
01/06	50	0,7	0,7	20	30	30	40	2,88					

Table 2 – Data for the waffle slab models											
Waffle slab - data from models  Lift column Nonlinearity coefficient Slab thickness f <sub>ct</sub> (MPa) Ceiling height											
Model	thickness (cm)	Slabs	Beams	Slab thickness (cm)	Slabs	Beams	Columns	for typical floor plan (m)			
02/01	40	0,3	0,4	21	30	30	40	3,24			
02/02	50	0,3	0,4	21	30	30	40	3,24			
02/03	40	0,3	0,4	23,5	30	30	40	3,24			
02/04	40	0,3	0,4	21	30	30	40	2,88			
02/05	50	0,3	0,4	23,5	30	30	40	2,88			

			Table 3 - I	Results from	models 01/	/01 e 01/02					
		Model 01/0	01				Model 01/	02			
Instability coefficient Service limit state - SLS					Inst	ability coeffici	ent	Service lim	it state - SLS		
Wind	Gamma Z	Alpha	Local disp.	Global disp.	Wind	Gamma Z	Alpha	Local disp.	Global disp.		
90° - 270°	1,297	1,262	0,12 (2120)	5,53 (2734)	90° - 270°	1,289	1,254	0,12 (2142)	5,39 (2805		
0° - 180°	1,265	1,186	0,09 (2705)	3,34 (4521)	0° - 180°	1,265	1,187	0,09 (2695)	3,32 (4552		
	R	M2M1 - 1,3	330		RM2M1 - 1,324						
	Quo	antity of co	lumns		Quantity of columns						
Concre	te volume (m <sup>:</sup>	3)	Area of formw	vork (m²)	Concre	te volume (m <sup>:</sup>	3)	Area of formwork (m²)			
Column	Total		Column	Total	Column	Total		Column	Total		
8561,9	15121,	7	36795,4	74365,1	8725,5	15284,	1	36735,6	74322,2		
Concrete volume rate Area of formwork rate				Concre	te volume rate	Э	Area of formwork rate				
56,62% 49,48%			6		57,09%		49,43%				

Table 4 - Results from models 01/03 e 01/04												
		Model 01/0	13				Model 01/	04				
Inst	ability coeffici	ent	Service limi	it state - SLS	Inst	ability coeffic	ient	Service lim	it state - SLS			
Wind	Gamma Z	Alpha	Local disp.	Global disp.	Wind	Gamma Z	Alpha	Local disp.	Global disp.			
90° - 270°	1,239	1,141	0,12 (2662)	4,45 (3399)	90° - 270°	1,271	1,216	0,11 (2449)	4,74 (3146)			
0° - 180°	1,213	1,069	0,07 (3452)	2,66 (5683)	0° - 180°	1,237	1,128	0,08 (3226)	2,76 (5399)			
	R	M2M1 - 1,2	77		RM2M1 - 1,318							
	Quo	antity of col	umns			Quantity of columns						
Concre	te volume (m³	3)	Area of formw	ork (m²)	Concre	ete volume (m	3)	Area of formwork (m²)				
Column	Total		Column	Total	Column	Total		Column	Total			
8561,9	15744,	2 3	36765,4	74353,3	8450,1	15714,	3	36230,0	77846,2			
Concre	Concrete volume rate Area of formwork rate				Concre	Concrete volume rate			Area of formwork rate			
54,38%			49,45%	ó		53,77%		46,54%				

Table 5 – Results from models 01/05 e 01/06												
		Model 01/0	05					Model 01/	06			
Inst	ability coeffici	ient	Service lim	it state - SLS		Inst	ability coeffic	ient	Service lim	it state - SLS		
Wind	Gamma Z	Alpha	Local disp.	Global disp.		Wind	Gamma Z	Alpha	Local disp.	Global disp.		
90° - 270°	1,172	0,976	0,10 (3328)	3,49 (4336)		90° - 270°	1,275	1,178	0,12 (2160)	5,21 (2859)		
0° - 180°	1,162	0,953	0,06 (5474)	2,13 (7113)		0° - 180°	1,298	1,110	0,16 (1517)	3,65 (4089)		
	R	RM2M1 - 1,1	90			RM2M1 - 1,357						
	Quo	antity of co	umns			Quantity of columns						
Concre	te volume (m	3)	Area of formw	rea of formwork (m²)			te volume (m	3)	Area of formwork (m²)			
Column	Total		Column	Total		Column	Total		Column	Total		
8561,9	15121,	7	36765,4	74365,1		5346,5	13420,	7	25285,9	67476,4		
Concre	te volume rat	е	Area of formw	ork rate		Concrete volume rate Area of formwork rate				ork rate		
	56,62%			,		39,84%			37,47%			

#### 4.2 Analysis results of models 02/01 to 02/05

The results obtained using the proposed design shown in Figure 3 and models described above were analyzed and are shown in Tables 6, 7 and 8.

As in the model with the prestressed slabs, increasing the thickness of the lift columns (stiff core) in the model with the waffle slabs (model 02/02) did not significantly decrease the  $\gamma_z$  coefficient; the reductions were approximately 0.694% (wind 90°-270°) and 0% (wind 0°-180°). Increasing the slab cover in model 02/03 resulted in decreases of the  $\gamma_z$  coefficient of approximately 3.392% (wind 90°-270°) and 3.014% (wind 0°-180°). The increase in weight due to the larger slab cover was offset by the greater stiffness as was discussed byFEITOSA and ALVES (2015) [6].

Decreasing the ceiling height of the floors in model 02/04 de-

creased the value of  $\gamma_z$  by approximately 4.086% (wind 90°-270°) and 3.632% (wind 0°-180°).

Finally, decreasing the size of the columns in model 02/05 caused a reduction of approximately 10.5% in the volume of concrete used for the columns and a reduction of approximately 6.22% in the formworks used for the columns compared to model 02/01. It is worth noting that the value of  $\gamma_z$  in model 02/05 is also less than the limit that is recommended by ABNT NBR 6118:2014 [2].

#### 5. Conclusões

The analysis of models of prestressed slabs and waffle slabs showed that increasing the thickness of the lift columns (stiff core) did not significantly reduce the  $\gamma_z$  instability coefficient.

Thicker prestressed slabs and a greater waffle slab cover

			Table 6 - I	Results from	models 02/	/01 e 02/02					
		Model 02/	וו				Model 02/	02			
Instability coefficient Service limit state - SLS					Inst	ability coeffici	ent	Service lim	it state - SLS		
Wind	Gamma Z	Alpha	Local disp.	Global disp.	Wind	Gamma Z	Alpha	Local disp.	Global disp.		
90° - 270°	1,297	1,280	0,14 (1821)	6,12 (2470)	90° - 270°	1,288	1,269	0,14 (1851)	5,94 (2546)		
0° - 180°	1,294	1,249	0,12 (2096)	4,04 (3758)	0° - 180°	1,294	1,248	0,12 (2097)	4,01 (3773)		
	R	M2M1 - 1,	345		RM2M1 - 1,335						
	Quo	antity of co	lumns			Quantity of columns					
Concre	te volume (m <sup>:</sup>	3)	Area of formw	ork (m²)	Concre	Concrete volume (m		3) Area of form			
Column	Total		Column	Total	Column	Total		Column	Total		
8744,8	13362,	8	37497,1	40303,7	8908,4	13525,	2	37467,3	40261,1		
Concrete volume rate Area of formwork rate				ork rate	Concre	te volume rat	Area of formw	ea of formwork rate			
65,44%			93,04%	6		65,87%		93,06%			

	Table 7 – Results from Models 02/03 e 02/04												
		Model 02/0	03					Model 02/	04				
Inst	ability coeffici	ient	Service lim	it state - SLS		Inst	ability coeffic	ient	Service lim	it state - SLS			
Wind	Gamma Z	Alpha	Local disp.	Global disp.		Wind	Gamma Z	Alpha	Local disp.	Global disp.			
90° - 270°	1,253	1,187	0,11 (2187)	5,14 (2939)		90° - 270°	1,244	1,173	0,11 (2268)	4,84 (3079)			
0° - 180°	1,255	1,172	0,09 (2704)	3,39 (4467)		0° - 180°	1,247	1,165	0,07 (3340)	3,15 (4734)			
	R	RM2M1 - 1,2	299			RM2M1 - 1,283							
	Quo	antity of co	umns			Quantity of columns							
Concre	te volume (m	3)	Area of formw	rea of formwork (m²)		Concrete volume (m³)		3)	Area of formwork				
Column	Total		Column	Total		Column	Total		Column	Total			
8744,8	14231,	5	37497,1	40287,8		8632,0	13747,	2	36957,7	39985,7			
Concre	Concrete volume rate Area of formwork rate					Concre	te volume rat	Area of formwork rate					
	61,45%			93,07%			62,79%		92,43%				

significantly reduced the  $\gamma_z$  coefficient. The greater vertical loads due to the thicker slabs are offset by the greater stiffness of the connections between the slabs and columns and also by the greater transverse bending stiffness. MARTINS (2001) [8] and FEITOSA and ALVES (2015) [6] obtained similar results.

Reducing the ceiling height between the floors in the models resulted in smaller  $\gamma_z$  coefficients due to the shorter unbraced lengths of the columns.

The application of a higher coefficient to represent the physical nonlinearity in prestressed slabs significantly reduced the  $\gamma_z$  coefficient; this reduction was the greatest of all of the models. Thus, it is interesting to study the use of higher values of the reduction coefficients than are indicated by the current standard given the lower amount of cracking that

Table 8 - Results from Modelo 02/05 Model 02/05 Instability coefficient Service limit state - SLS Global Gamma Z **Alpha** disp. disp. 90° - 270° 1,285 1,251 0,12 (2061) 5,39 (2768) 0° - 180° 1,291 1,216 0,10 (2523) 3,50 (4260) RM2M1 - 1,355 **Quantity of columns** Concrete volume (m³) Area of formwork (m²) Total Total 7824,5 13904,5 35163,9 38168,8 Concrete volume rate 56,27% 92,13%

occurs in prestressed elements than in reinforced concrete elements. A comparison of the total volume of concrete used in models 01/06 and 02/05 revealed that model 01/06 used approximately 3.5% less concrete than model 02/05. A similar comparison of the concrete volume of the columns shows that model 01/06 used approximately 31.6% less concrete for the columns. Thus, using a higher coefficient of physical nonlinearity for the prestressed slab makes this type of system competitive with waffle slabs in terms of the required volume of concrete for tall and slender buildings.

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