

# Numerical Analysis of Swirl Effects on Conical Diffuser Flows

Eron Tiago Viana Dauricio<sup>1</sup>, Claudia Regina de Andrade<sup>1</sup>

**ABSTRACT:** The present paper focuses on the effect of swirl on important parameters of conical diffusers flows such as static pressure evolution, recirculation zones and wall shear stress. Governing equations are solved using a software based on the finite volume method. Moreover, turbulence effects are taken into account employing the  $k-\epsilon$  RNG model with an enhanced wall treatment. The Reynolds number has been kept constant at  $10^5$ , and various diffuser geometries were simulated, maintaining a high area ratio of 7 and varying the total divergence angle ( $16^\circ$ ,  $24^\circ$ ,  $40^\circ$ , and  $60^\circ$ ). Results showed that the swirl velocity component develops into a Rankine-vortex type or a forced-vortex type. In the former, swirl is not effective to prevent boundary layer separation, and a tailpipe is recommended to allow a large-scale mixing to enhance the pressure recovery process. In the latter case, boundary layer separation is prevented but an intermediary recirculation zone appears. Higher pressure recovery is attained at the exit of the diffuser with swirl addition, without the need of a tailpipe. Results also suggest that there is an imposed swirl intensity where the energy losses are minimum thus leading pressure recovery to an optimum level.

**KEYWORDS:** Static pressure recovery, Wide-angle diffuser, Swirl intensity, Radial pressure gradient, Intermediary recirculation zone.

## INTRODUCTION

Diffusers are widely used in many industrial devices and applications in order to convert kinetic energy into static pressure. Examples include applications in gas turbines, water turbines draft tubes, piping systems, and more. In real flows, however, this conversion process is taken at the cost of total energy, which decreases because of dissipative mechanisms, and the aim is always to design a diffuser with the best possible efficiency.

For uniform or fully developed inlet flows, the changes in performance of diffusers due to geometry are well known and these data are generally written in chart form to simplify the design process, where a coefficient of performance is plotted against area and/or length ( $L$ ) ratio of the diffuser (ESDU 1990). However, in practical situations, because of physical constraints, one cannot always design and build a diffuser with optimum performance according to its geometry (*i.e.* area ratio or length constraint), and generally the diffuser will have angles wider than the optimum. This may cause a rapid growth in boundary layer because of the strong pressure gradient, and the boundary layer may separate creating a recirculating region, decreasing the effective flow area and increasing the energy losses. Therefore, ways of achieving improved diffuser performance under non-optimum geometries must be accomplished. Various methods for improving performance have been proposed and attempted, such as application of suction, injection of a secondary flow, introduction of vanes to divide the diffuser into several smaller angle diffusers, or the introduction of vortex and rotational flow at the inlet. The latter is of particular importance because it is present in many industrial flows; therefore, the capacity to predict and understand the physical phenomenon behind this type of flow is of paramount importance.

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**Received:** Apr. 28, 2016 | **Accepted:** Ago. 20, 2016

The addition of swirl to the flow induces radial pressure gradients and centrifugal forces that push the fluid towards the diffuser wall, preventing the excessive growth of the boundary layer and counteracting the tendency of flow separation, thus increasing the diffuser efficiency and performance. However, the addition of swirl also decreases the axial momentum near the centerline, which is expected from the analysis of mass conservation; depending on the swirl intensity, there may appear a central recirculating zone. The phenomenon giving rise to this central recirculating zone is called vortex breakdown.

Extensive theoretical and experimental studies and reviews on vortex stability and breakdown have been carried out in the past by Leibovich (1984), Falser and Leibovich (1977), Escudier (1988), Escudier and Keller (1985), Sloan *et al.* (1986) and Chen *et al.* (1997), generally in straight tube geometries. Sarpkaya (1974) performed experiments and studies on this theme in diverging tube geometries, which accounts for the influence of pressure gradient in the phenomenon. As of swirl addition to the flow for performance improvement in conical diffusers, many experimental studies have been carried out, for example, Neve and Wirasinghe (1978), Senoo *et al.* (1978), Okhio *et al.* (1983) and McDonald *et al.* (1971), in which they all mention the appearance of a central recirculating zone depending on the swirl intensity. Numerical studies have also been developed to predict swirling flows, such as the predictions of Cho and Fletcher (1989), Armfield *et al.* (1990), Okhio *et al.* (1986) and Pordal *et al.* (1993). Nonetheless, the experimental studies that have been carried out so far focus mostly on the performance analysis and improvement, using pressure recovery coefficient and efficiency parameters. Therefore vortex breakdown phenomenon is actually avoided instead of discussed. The present study aims at the analysis of the effect of swirl addition to the conical diffuser flow pattern, including the regime when vortex breakdown occurs and its relation to static pressure evolution, boundary layer separation and radial pressure gradient. Present results also allow to identify the relationship between swirl velocity profile and diffuser wall slope.

## MATERIAL AND METHODS

### GOVERNING EQUATIONS

Governing equations (cylindrical coordinates) for an incompressible axisymmetric steady turbulent flow can be given as:

$$\frac{1}{r} \frac{\partial (r \bar{v}_r)}{\partial r} + \frac{\partial \bar{v}_x}{\partial x} = 0 \quad (1)$$

$$\begin{aligned} \frac{1}{r} \frac{\partial (r \bar{v}_r \bar{v}_r)}{\partial r} + \frac{\partial (\bar{v}_r \bar{v}_x)}{\partial x} - \frac{\bar{v}_\theta \bar{v}_\theta}{r} + \frac{1}{\rho} \frac{\partial \bar{p}}{\partial r} = \\ = f_r + \frac{1}{r} \frac{\partial [r (\bar{\tau}_{rr} - \bar{\tau}_{rr}^R)]}{\partial r} + \frac{\partial (\bar{\tau}_{r\theta} - \bar{\tau}_{r\theta}^R)}{\partial x} - \frac{1}{r} (\bar{\tau}_{\theta\theta} - \bar{\tau}_{\theta\theta}^R) \end{aligned} \quad (2)$$

$$\begin{aligned} \frac{1}{r^2} \frac{\partial (r^2 \bar{v}_r \bar{v}_\theta)}{\partial r} + \frac{\partial (\bar{v}_x \bar{v}_\theta)}{\partial x} = \\ = f_\theta + \frac{1}{r^2} \frac{\partial [r^2 (\bar{\tau}_{r\theta} - \bar{\tau}_{r\theta}^R)]}{\partial r} + \frac{\partial (\bar{\tau}_{x\theta} - \bar{\tau}_{x\theta}^R)}{\partial x} \end{aligned} \quad (3)$$

$$\begin{aligned} \frac{1}{r} \frac{\partial (r \bar{v}_r \bar{v}_x)}{\partial r} + \frac{\partial (\bar{v}_x \bar{v}_x)}{\partial x} + \frac{1}{\rho} \frac{\partial \bar{p}}{\partial x} = \\ = f_x + \frac{1}{r} \frac{\partial [r (\bar{\tau}_{rx} - \bar{\tau}_{rx}^R)]}{\partial r} + \frac{\partial (\bar{\tau}_{xx} - \bar{\tau}_{xx}^R)}{\partial x} \end{aligned} \quad (4)$$

where:  $\bar{v}_r$ ,  $\bar{v}_\theta$  and  $\bar{v}_x$  are the mean components of the velocity in the radial, tangential and axial direction, respectively;  $\bar{\tau}_{ij}$  is the symmetric viscous stress tensor;  $\bar{\tau}_{ij}^R = \bar{v}_i \bar{v}_j$  represent the Reynolds-stress tensor;  $f_i$  are the components of external forces, which are zero in this case.

For the axisymmetric flow considered, the viscous stress tensor components are given by:

$$\bar{\tau}_{rr} = 2\nu \frac{\partial \bar{v}_r}{\partial r}; \quad \bar{\tau}_{\theta\theta} = 2\nu \frac{\bar{v}_r}{r}; \quad \bar{\tau}_{xx} = 2\nu \frac{\partial \bar{v}_x}{\partial x} \quad (5)$$

$$\bar{\tau}_{r\theta} = \nu r \frac{\partial}{\partial r} \left( \frac{\bar{v}_\theta}{r} \right); \quad \bar{\tau}_{x\theta} = \nu \frac{\partial \bar{v}_\theta}{\partial x}; \quad \bar{\tau}_{rx} = \nu \left( \frac{\partial \bar{v}_x}{\partial r} + \frac{\partial \bar{v}_r}{\partial x} \right) \quad (6)$$

where:  $\nu = \mu/\rho$ .

These equations can be easily derived from the conservation form of the Navier-Stokes equations using the proper operations for the  $\nabla$  operator in cylindrical coordinates (see, for example, Bird *et al.* 2002).

## TURBULENCE MODELING

Because of the Reynolds-averaging process and the consequent appearance of the Reynolds-stress tensor, we now have 4 equations and 10 unknowns (*i.e.* pressure, 3 velocity components and the 6 components of the Reynolds-stress tensor), and thus a closure problem. To overcome the closure problem, we need to correlate the Reynolds-stress tensor components to known quantities. The turbulence model used in this study lies under the eddy-viscosity turbulence model category, which makes use of the Boussinesq hypothesis and is called the k- $\epsilon$  RNG model (Yakhot and Orszag 1986), derived using a statistical technique called renormalization group. It was used with a modification to account for swirling flows, as described in Galván *et al.* (2011). As shown by the research of Escue and Cui (2010), the k- $\epsilon$  RNG model yields good results for the prediction of mean velocity components under low-to-moderate swirl numbers.

## SWIRL NUMBER

Swirling flows are characterized by a tangential velocity component in addition to the axial velocity component of swirl-free flows. This can be accomplished in a number of ways, for example, passing the flow radially through blades and controlling the amount of swirl addition by changing the angle of the blades, or passing the flow through a rotating honeycomb device. Different types of swirl addition may create different characteristics on the swirling flow. There may exist a Rankine-vortex type, where a core region of the flow is dominated by viscous effects and a forced-vortex type is present as well as an outer region consisting of a free-vortex type. There may exist a full forced-vortex type (solid-body rotation) where the tangential velocity linearly increases with radius (Najafi *et al.* 2011). In this paper, we use the definition of swirl number,  $S$ , as being the ratio between the tangential momentum flux and the axial momentum flux, as given by Rocklage-Marliani *et al.* (2003):

$$S = \frac{2\pi\rho \int_0^R \overline{v_x} \overline{v_\theta} r^2 dr}{2\pi\rho R \int_0^R \overline{v_x} r dr} \quad (7)$$

## NUMERICAL PROCEDURE

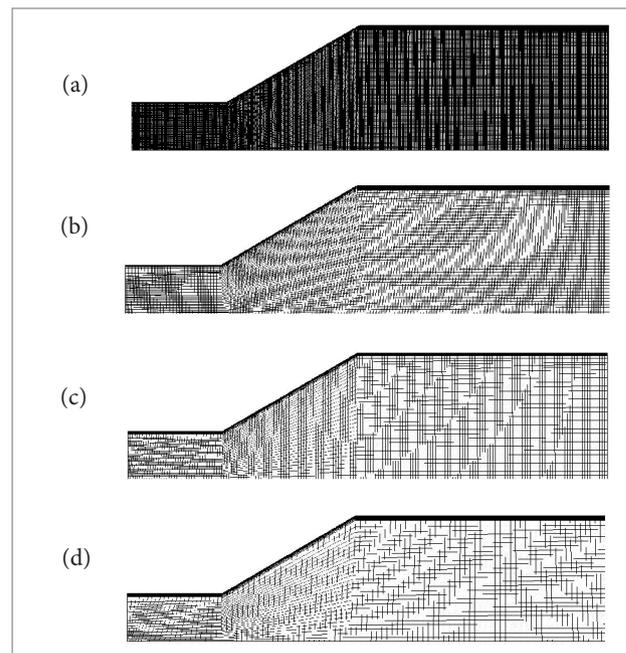
Diffuser turbulent flow was simulated using the software ANSYS 16.1, a finite volume-based solver employing the k- $\epsilon$  RNG model with an adaption for swirl-dominated flows. The SIMPLE algorithm was used as a strategy for the velocity-pressure

coupling. Both the convection and diffusion terms were discretized using a 2nd-order upwind scheme. All simulations were carried out until the maximum residuals of all variables reached a value of  $10^{-5}$ .

Different geometries of conical diffusers were tested with an area ratio equal to 7 and varying total angles of 16°; 24°; 40°; and 60°. Meshes for each geometry were generated using 45 divisions in the radial direction, while the divisions in the axial one ranged from 150 to 300, depending on the diffuser length, which is a function of the total angle of divergence. It is worth mentioning that it is important for the grid to be relatively fine in the axial direction because of the swirl decay, which also needs to be predicted in order to accomplish accurate results. The  $y$ -value was within the recommended range for the turbulence model currently used (Bigarella and Azevedo 2006).

Near-Cartesian meshes were employed, with average orthogonal quality of about 0.99 and average skewness less than 0.2. Skewness is most affected in the divergence region of the diffuser geometry. A grid refinement study was performed in terms of the grid size, using the 60°-diffuser. Four meshes were tested, which are shown in Fig. 1. The basic properties of each mesh are summarized in Table 1. As the problem is axisymmetric, only half diffuser needs to be drawn and numerically solved.

An incompressible flow with inlet swirl number of 0.3 was simulated for this grid sensitivity analysis. Swirl decay throughout



**Figure 1.** Four tested grids in the sensitivity analysis. (a) Grid #1; (b) Grid #2; (c) Grid #3; (d) Grid #4.

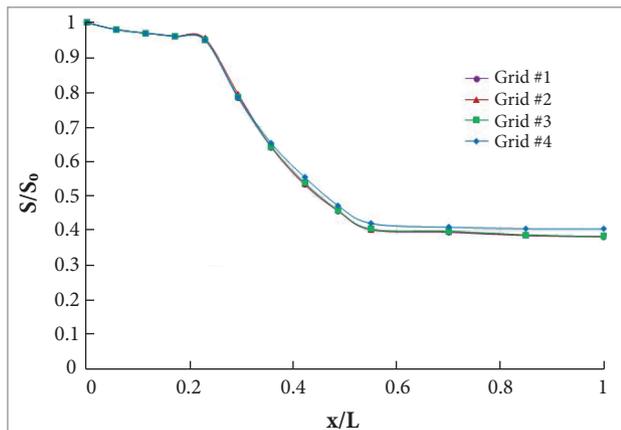
**Table 1.** Basic properties of the four tested grids.

	Grid #1	Grid #2	Grid #3	Grid #4
Axial divisions	1,000	300	150	80
Radial divisions	85	60	45	40
Minimum orthogonal quality	0.87	0.86	0.84	0.84
Maximum skewness	0.23	0.24	0.26	0.31

the diffuser can be analyzed, as the number of axial divisions also varies for each mesh.

Swirl number across sections inside the diffuser domain was calculated according to Eq. 7, and the predicted swirl decay throughout the geometry is shown in Fig. 2 for all grids. It can be seen from the inlet to the mid-length of the diffuser that results for swirl decay predicted for all grids firmly agreed, with little discrepancy. However, from the mid-length to the outlet of the diffuser, discrepancies appeared in the results, with grid #4 predicting the softer swirl decay. Table 2 summarizes the grid sensitivity results presenting the maximum difference which each grid relatively exhibited in relation to each other for the swirl decay prediction.

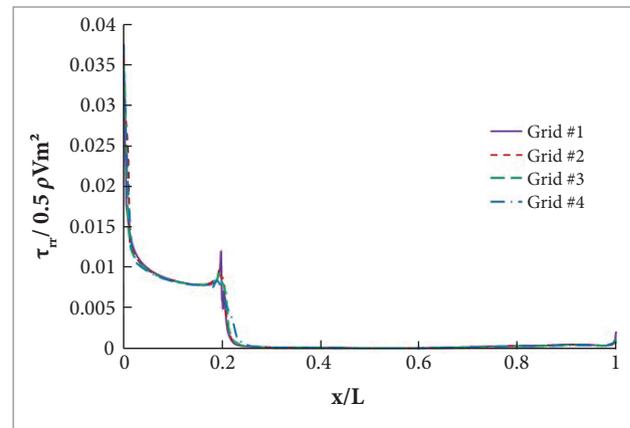
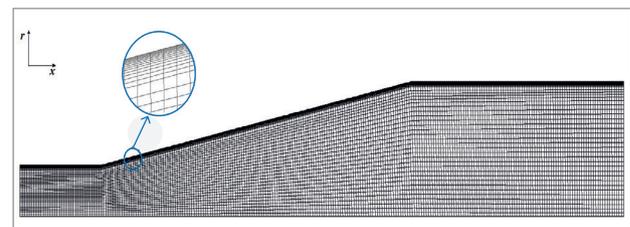
Assuming the results of grid #1 as being the more reliable and accurate because it is the finest grid, the maximum difference of the other grids relative to grid #1 was evaluated. Grids #2 and #3 presented a very small difference, less than 1.5%, while grid #4 presented a difference greater than 6% and therefore was discarded. Between grids #2 and #3, the latter was chosen for the simulations because it is coarser

**Figure 2.** Comparison of the swirl decay calculation for all tested grids.**Table 2.** Maximum difference of the four tested grids relative to each other.

	Grid #1	Grid #2	Grid #3	Grid #4
Grid #1	-	1.39%	1.22%	6.1%
Grid #2	1.39%	-	0.98%	5.76%
Grid #3	1.22%	0.98%	-	5.63%
Grid #4	6.1%	5.76%	5.63%	-

than the first, which would save computational effort. Although this analysis was done using the 60°-diffuser, the grids for the other geometries had the same axial divisions, proportionally (*i.e.* the same divisions per length ratio have been kept). As the diameters do not vary, the same number of radial divisions was kept for all grids, as mentioned before. Because calculation of the swirl decay does not contain information regarding the boundary layer region, the wall shear stresses along the diffuser were also analyzed. Figure 3 shows the results of wall shear stresses for all tested grids, where it can be seen that they all predicted a result very close to each other, which means that all grids are fine enough in the boundary layer region.

Figure 4 shows the computational mesh for the 24°- diffuser with a close at the boundary layer region.

**Figure 3.** Comparison of the wall shear stress calculation for all tested grids.**Figure 4.** 24°- diffuser mesh and boundary layer zoom.

## BOUNDARY CONDITIONS

For the inlet boundary, velocity magnitude was fixed allowing a Reynolds number of about  $10^5$ . The velocity direction was given in terms of a unit vector in the direction of velocity so the tangential component could be easily changed to increase or decrease swirl intensity. Inlet boundary conditions for turbulent parameters were set in terms of the turbulence intensity,  $I = v''/\bar{v}$ , and turbulent viscosity ratio,  $\mu^T/\mu$ . The latter is directly proportional to the turbulent Reynolds number,  $Re^T = \rho k^2/\epsilon\mu$ , and therefore contains the information needed for  $k$  and  $\epsilon$  calculation. In the present paper, turbulence intensity and turbulent viscosity ratio were set at 5 and 10, respectively. The operating (“external”) pressure was prescribed at sea-level conditions. The density was constant and known, with a value corresponding to 1 atm and temperature of 500 K, *i.e.*  $\rho = 0.71 \text{ kg/m}^3$ . These conditions were chosen to better simulate the environment of a diffuser in a gas turbine, which is the main motivation for this study, although it could be extended to any swirling flow in conical diffuser since the non-dimensional parameters match has been satisfied. The outlet boundary condition was set at zero gauge static pressure. This allows the CFD software to accommodate the pressure values at inlet and outlet so the velocity and mass flow conditions are properly satisfied. At the centerline, axisymmetric condition has been imposed. The no-slip boundary condition has been prescribed at the wall surface.

## RESULTS AND DISCUSSION

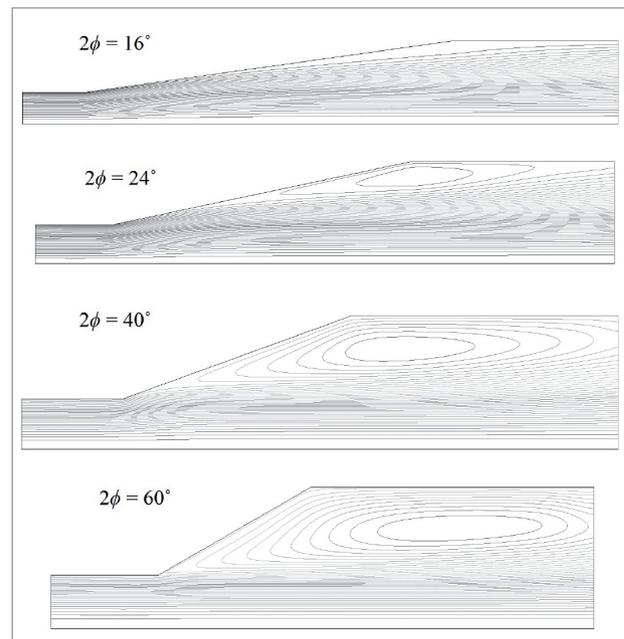
Three values of swirl number (Eq. 7) were herein tested: (i)  $S = 0$  (no swirl), (ii)  $S = 0.3$ , and (ii)  $S = 0.6$ . Firstly, the behavior of flow streamlines was investigated, followed by the static pressure evolution through the diffuser length. Then, the radial pressure gradient and wall shear stresses were also shown.

### STREAMLINES

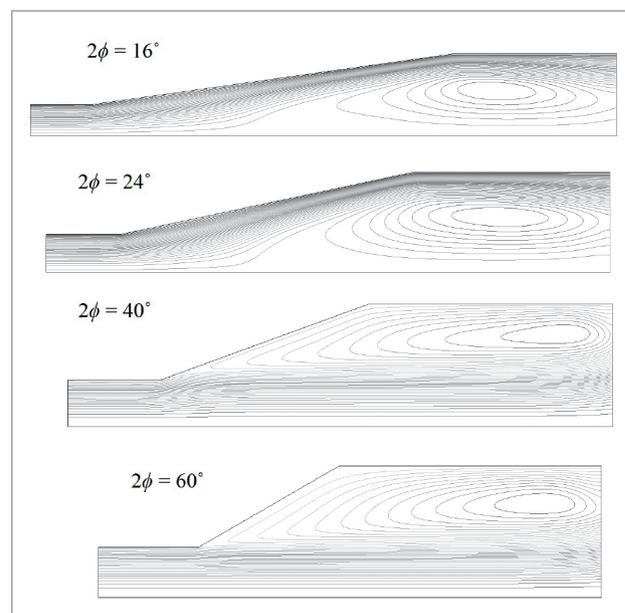
Stream function contours are plotted for all cases, and the results are shown in Figs. 5, 6 and 7. It can be seen that, if the flow has no swirl, there exist flow separation for all tested angles, and the recirculation zone size is proportional to the total angle of the diffuser, being broader when the angle is wider. In the case of swirl addition, some interesting phenomena arise, as follows:

- For  $S = 0.3$ , a central recirculating zone appears in the lower angle geometries (*i.e.*  $16^\circ$  and  $24^\circ$ ), indicating the

occurrence of vortex breakdown, although separation of the boundary layer is prevented in these cases. For the 2 wider angles, the separation of boundary layer still occurs. However, swirl delays the growth of boundary layer due to centrifugal forces, and the separation point occurs downstream. This can be confirmed by noting that the recirculating bubble appears further downstream for those cases.

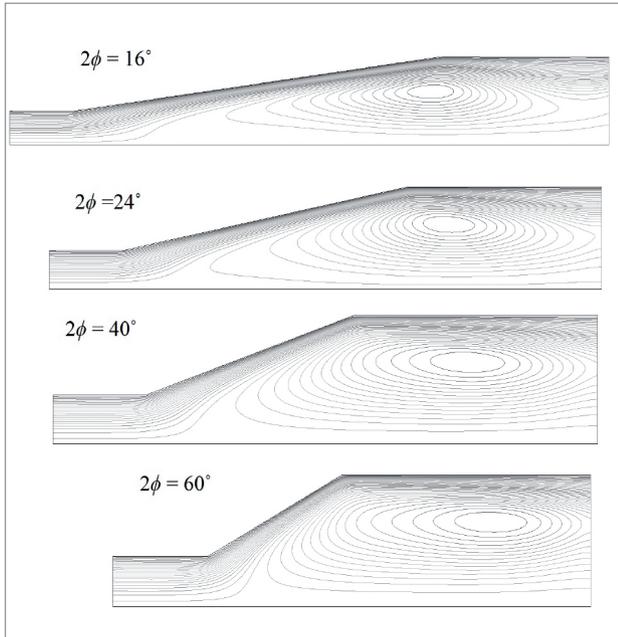


**Figure 5.** Streamline contours, no swirl.

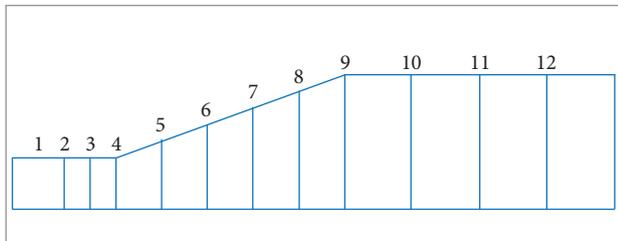


**Figure 6.** Streamline contours for  $S = 0.3$ .

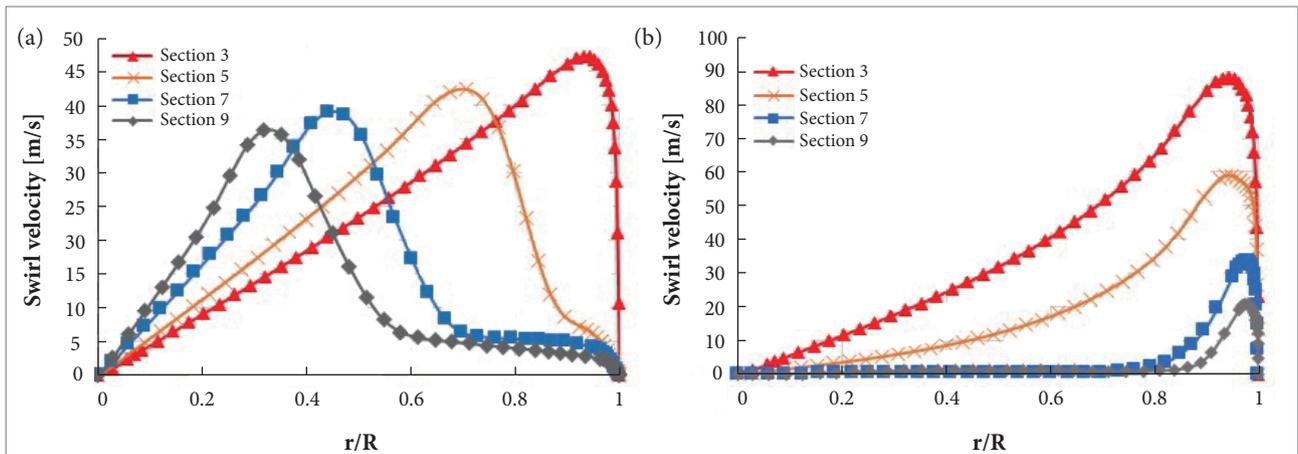
- For  $S = 0.6$ , there exist a central recirculation zone for all tested geometries, as shown in Fig. 7. Comparing the cases for the 16- and 24°- diffusers, it can be seen



**Figure 7.** Streamline contours for  $S = 0.6$ .



**Figure 8.** Cross-sections used for velocity profile plots and integrated-weighted-area quantities.



**Figure 9.** Swirl velocity profiles for 60°- diffuser. (a)  $S = 0.3$ ; (b)  $S = 0.6$ .

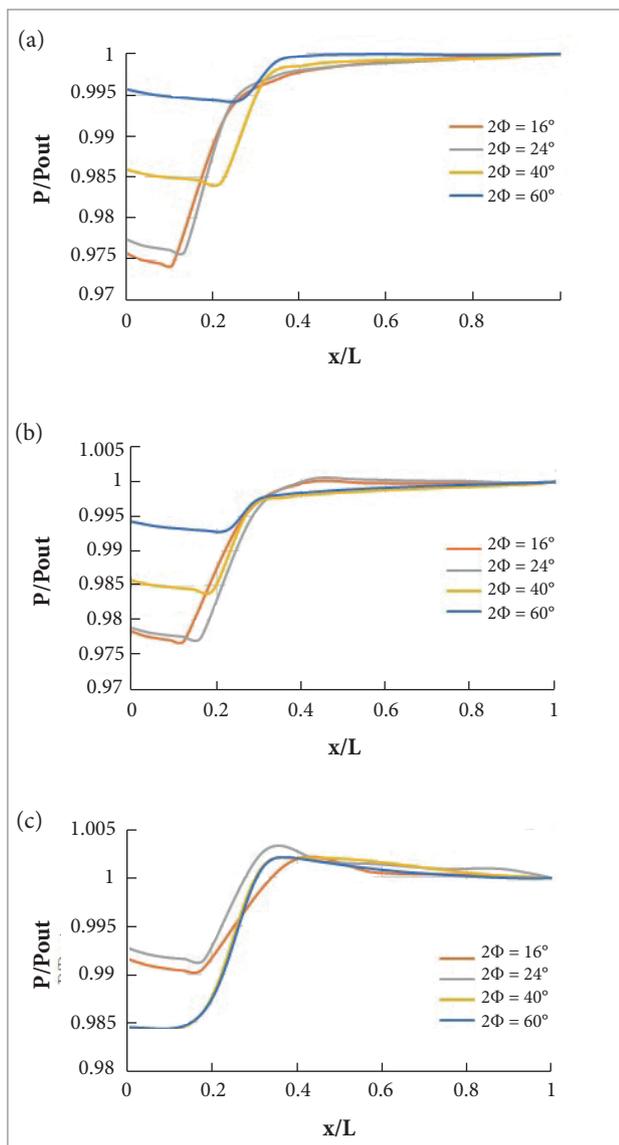
that the recirculation zone increases with increasing swirl intensity.

To further analyze this recirculation zone appearing inside the diffuser, the swirl velocity profile for various sections throughout the diffuser length is plotted against the normalized radius. The sectional planes are indicated in Fig. 8 and, for the various diffusers, they are placed at the same  $x_{diff}/L_{diff}$  so a concise comparison can be made among the different geometries. Figure 9 presents the swirl velocity profile along sections 3, 5, 7 and 9, in the case of the diffuser with total angle of 60°, for both swirl numbers 0.3 and 0.6. For  $S = 0.3$ , it can be noted that the swirl velocity profile develops into a Rankine-vortex type inside the diffuser (Najafi *et al.* 2011), although the boundary conditions at the inlet are that of a forced-vortex type, as can be seen for the velocity profile at section 3. The swirl is too weak for the rapid area growth in this case, so the tangential velocity component does not reach the region near the wall because of weak centrifugal forces, achieving a Rankine-vortex type profile. Thus, the swirl is not effective in preventing boundary-layer growth and separation in this case, and the axial momentum near the wall is low. On the other hand, for  $S = 0.6$ , swirl effect seems to induce centrifugal forces high enough to carry the tangential component to the near-wall region and thus prevent the boundary-layer separation by enhancing momentum transport. In this case, the axial momentum is higher near the wall than when it is close to the centerline, as would be expected by a mass conversation analysis. This makes a recirculation region to appear in the intermediary region instead of near the wall. In addition, the recirculation zone occurring in the intermediary zone, due to the decrease in axial momentum,

forces the tangential momentum to concentrate in the region near the wall, as shown in Fig. 9b.

### STATIC PRESSURE EVOLUTION

Because swirl addition induces radial pressure gradients, the static pressure is taken as an area-weighted average across the sections presented in Fig. 8 instead of the value in the centerline/wall, as it is usual for the swirl-free case (where the pressure is assumed constant along cross-section). The static pressure evolution is presented in Fig. 10 and has been normalized by the static pressure at the tailpipe outlet.

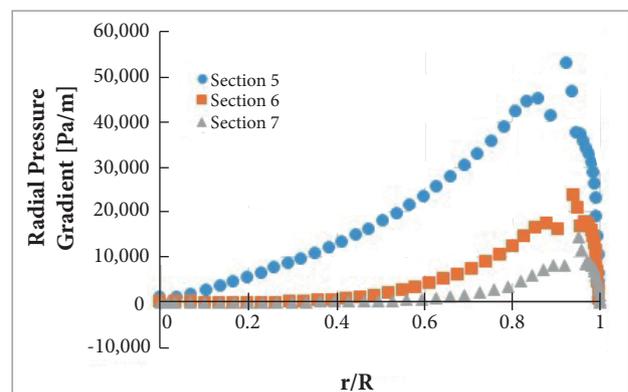


**Figure 10.** Static pressure evolution throughout the diffuser length at different divergence angles. (a) No swirl; (b)  $S = 0.3$ ; (c)  $S = 0.6$ .

In the swirl-free case, Fig. 10a shows that, for all geometries, there is still pressure recovery after the diffuser outlet. This is due to a large-scale mixing in the tailpipe, which converts dynamic pressure into static pressure, as discussed in the literature (Miller 2009). For the case in which  $S = 0.3$ , the highest static pressure is achieved at the end of the diffuser in the 16- and 24°- geometries, followed by a decrease in the tailpipe. For the 40- and 60°- geometries the pressure still rises after the diffuser due to the large-scale mixing. In the former case, the increase in static pressure due to large-scale mixing is surpassed by the decrease due to losses as a consequence of dissipative mechanisms (wall friction), and therefore the static pressure experiences a net decrease in the tailpipe. For the case in which  $S = 0.6$ , all geometries present the same behavior for the static pressure, occurring a maximum recovery at the end of the diffuser domain, followed by a decrease through the tailpipe. This is clearly related with the region where the recirculation zone takes place. When it occurs in the intermediary portion of the cross-section, the centrifugal forces pushing the fluid towards the wall are strong, and thus the wall friction losses overcome the pressure recovery due to mixing, causing a net effect of the static pressure decrease. However, when recirculation appears near the wall, the wall friction is low due to the boundary layer separation and therefore the pressure recovery due to large-scale mixing overcomes the pressure loss induced by friction effect.

### RADIAL PRESSURE GRADIENT AND WALL SHEAR STRESS

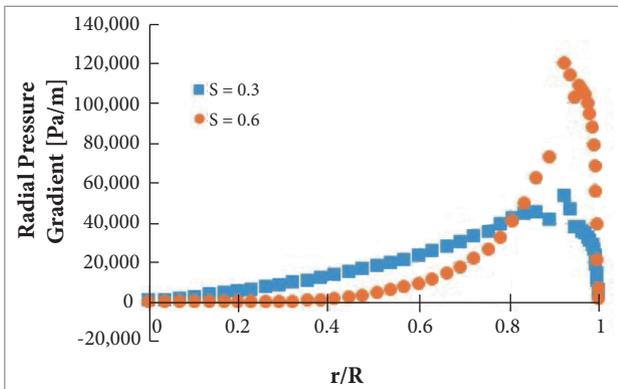
Figure 11 shows the plot of the radial pressure gradient in sections 5, 6 and 7 (Fig. 8) inside the diffuser domain



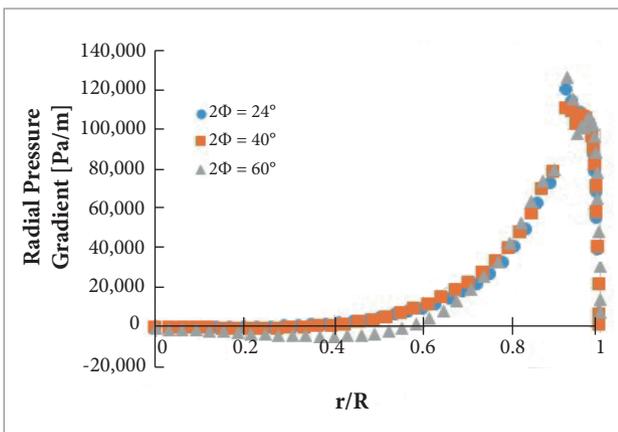
**Figure 11.** Radial pressure gradient for 3 geometry sections at  $S = 0.3$  and  $2\phi = 24^\circ$ .

for the total divergence angle of  $24^\circ$  and swirl number 0.3. Comparing with Fig. 9b, where the profile remains as a forced-vortex type, we can see that the radial pressure gradient qualitatively follows the swirl velocity profile, thus ensuring that this pressure gradient is induced by swirl addition. Figure 12 presents the radial pressure gradient (for the same geometry —  $2\phi = 24^\circ$ ) at 2 different swirl numbers, while Fig. 13 compares the behavior of radial pressure gradient at different diffuser divergence angles at constant swirl number. It can be seen that the radial pressure gradient value is almost exclusively dependent on the swirl number, and not on the divergence angle, and higher levels of swirl will cause stronger radial pressure gradients.

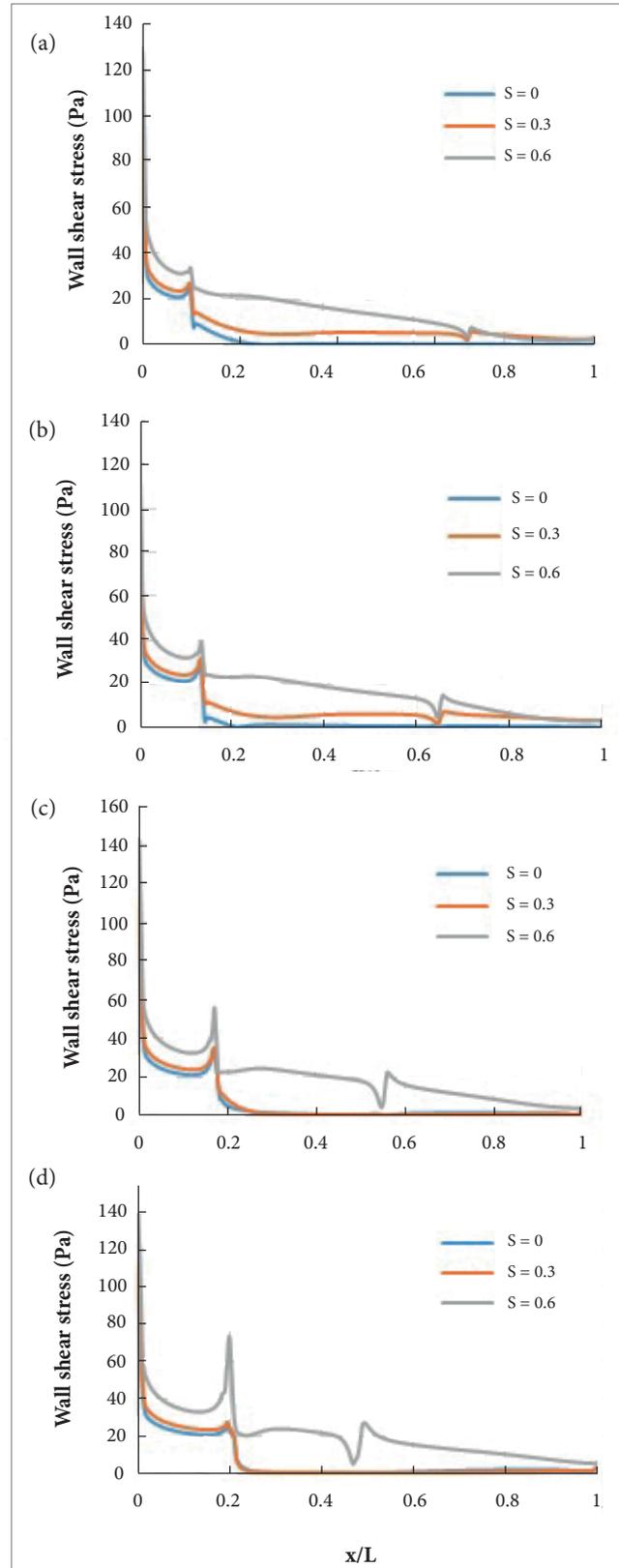
Figure 14 shows the wall shear stress for all tested geometries, with varying swirl numbers. Comparing with figures of radial pressure gradient, we can clearly see a correlation between these 2 quantities. As radial pressure gradient intensifies, the wall shear stress also increases. Furthermore, the wall shear



**Figure 12.** Radial pressure gradient for section 5 (geometry  $2\phi = 24^\circ$ ) and 2 different swirl numbers.



**Figure 13.** Radial pressure gradient for  $S = 0.6$  and 3 different divergence angles.



**Figure 14.** Wall shear stress along the diffuser length. (a)  $2\phi = 16^\circ$ ; (b)  $2\phi = 24^\circ$ ; (c)  $2\phi = 40^\circ$ ; (d)  $2\phi = 60^\circ$ .

stress is much more influenced by the swirl number than by the total divergence angle. This is the same behavior observed in the radial pressure gradient distributions.

The discussion made about the swirl velocity profiles is also implicit from the plots of wall shear stress. For the cases where it develops into a Rankine-vortex profile, the swirl velocity component near the wall is very low, and the wall shear stress almost vanishes in this region. On the other hand, when it remains as a forced-vortex type, the wall shear stresses are high close the wall surface.

## CONCLUSIONS

The present study analyzed the influence of swirl addition in the streamline pattern, pressure recovery, pressure gradient, and wall shear stress in a conical diffuser flow. The fact that a central recirculation zone appears in these flows is related to the swirl velocity profile developed inside the diffuser domain. If the swirl intensity is low relatively to the wall divergent angle, the swirl velocity profile develops into a Rankine-vortex profile and thus it is not effective in preventing boundary layer growth and separation. On the other hand, if the swirl intensity is high enough relatively to the wall divergent angle, the swirl velocity profile remains as a forced-vortex type profile and thus prevents boundary layer separation due to: (i) centrifugal forces pushing the fluid toward the wall; and (ii) increase in turbulence intensity in this region, enhancing momentum transport. However, in the last case, the swirl intensity showed also high enough to allow vortex breakdown to occur, generating a central recirculation zone. Although other researchers observed this recirculation zone in their experiments on conical diffuser flows, this relationship between swirl velocity profile and wall diffuser slope has not been previously mentioned. The results also suggest that there is an optimum swirl intensity where both boundary layer separation and vortex breakdown are prevented, avoiding a decrease in diffuser performance due to energy losses. Moreover, this optimum swirl intensity shall be related to the wall slope (*i.e.* diffuser geometry).

An assessment of static pressure evolution throughout the diffuser led to the following conclusions. When the swirl velocity profile remains as a forced-vortex type, the wall shear stresses are high due to the centrifugal forces pushing the fluid toward the wall, and thus the losses because of friction overcome the pressure recovery due to a large-scale mixing through the tailpipe, resulting in a net decrease in static pressure through the tailpipe. However, when the swirl velocity profile develops into a Rankine-vortex type inside the diffuser, the wall shear stresses are low due to separation of boundary layer, and the pressure recovery because of large-scale mixing overcomes the losses due to wall friction, and the pressure still rises throughout the tailpipe. This suggests that, if an optimum swirl intensity is achieved, which prevents both separation and vortex breakdown from occurring, there would be no need of a tailpipe to increase static pressure through a large-scale mixing, as it is usual in practical applications.

Radial pressure gradient and wall shear stresses qualitatively follow the swirl velocity profile. It is indeed expected, as the swirl component is the cause of the appearance of radial pressure gradients and centrifugal forces, which, in turn, moves the fluid to the wall, increasing velocity gradients and thus the wall shear stresses. The radial pressure gradient as well as the wall shear stress are much more dependent on the swirl intensity than on the diffuser geometry (*i.e.* total divergence angle).

## ACKNOWLEDGEMENTS

The authors would like to acknowledge the Conselho Nacional de Desenvolvimento Científico e Tecnológico – Brazil, for their support to this study.

## AUTHOR'S CONTRIBUTION

Andrade CR conceived the idea and co-wrote the main text. Daurício ETV performed the numerical simulations and built the required figures. Conclusions and discussions were prepared together.

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